



Nuclear EOS, the bridge between mini-merger and giant-merger

Zhigang Xiao

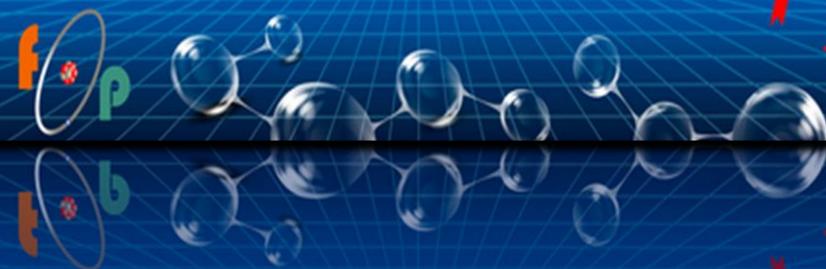
Department of Physics, Tsinghua University

原子核
简单
对称
美

原子核科学国际会议：简单-对称-美
恭贺有马朗人先生米寿
上海，2018年9月26日-28日



International Symposium of Nuclear Science: Simplicity, Symmetry, and Beauty
In honor of the Rice (米) Age of Professor Akito Arima
September 26-28, 2018, Shanghai



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1 Introduction (4')

2 Isospin transport in HIC and Isospin Chronology

2.1 Isospin dependent particle emission hierarchy (3')

2.2 Long time isospin-drift process and $E_{\text{sym}}(\rho)$ (3')

2.3 Isospin Chronology with HIRA^{TU}: future plan (4')

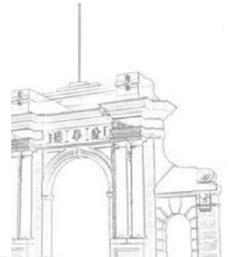
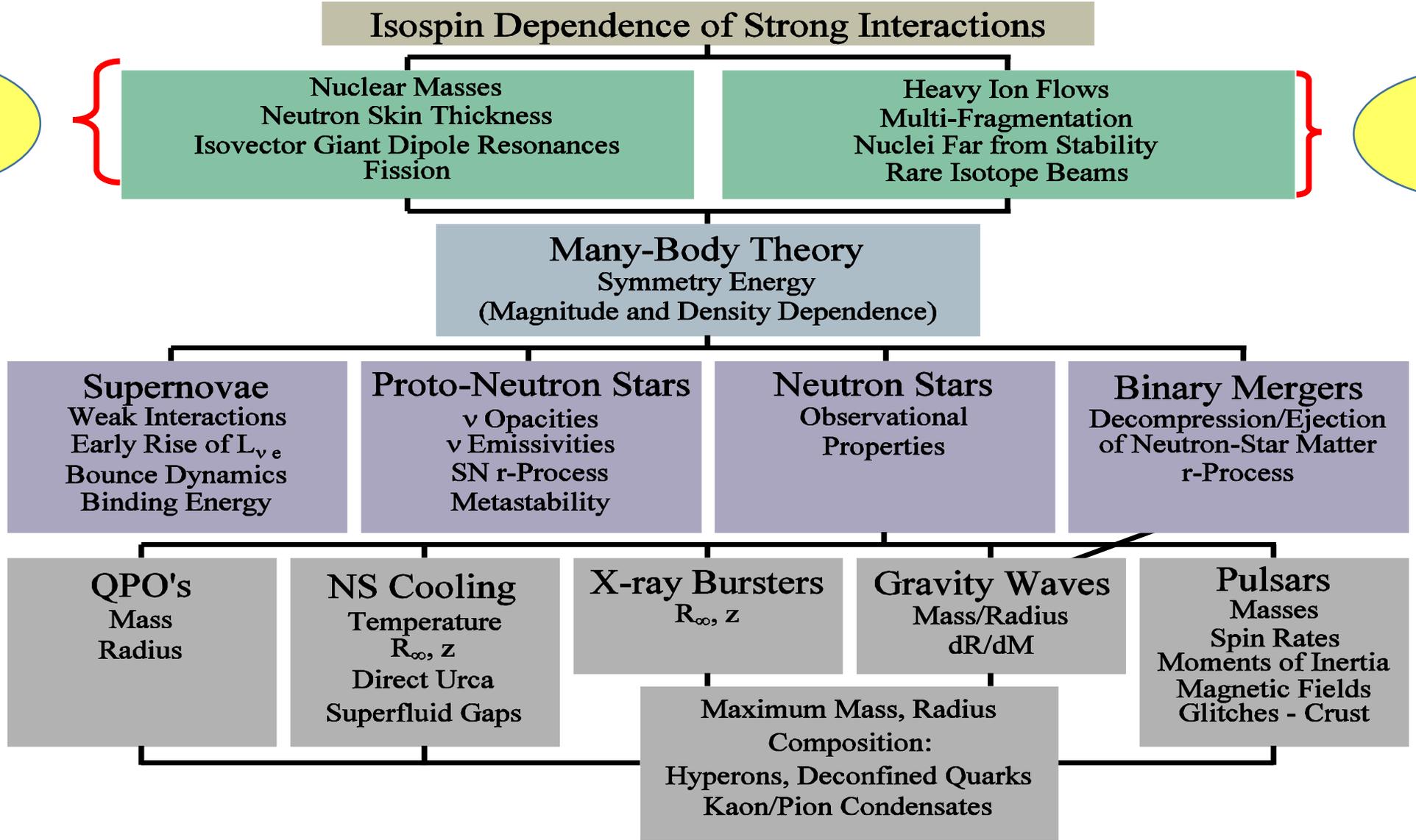
3 Isovector orientation effect of deuteron: A new tool to constrain $E_{\text{sym}}(\rho)$ (2')

4. Summary (1')

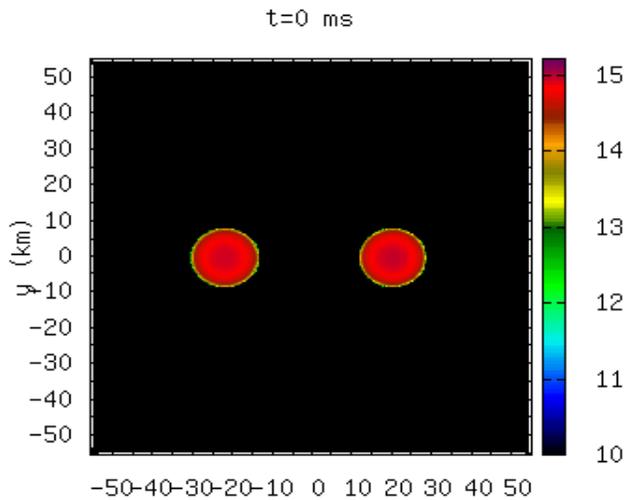
Nuclear Symmetry Energy

Nuclei Properties

Nuclear reactions

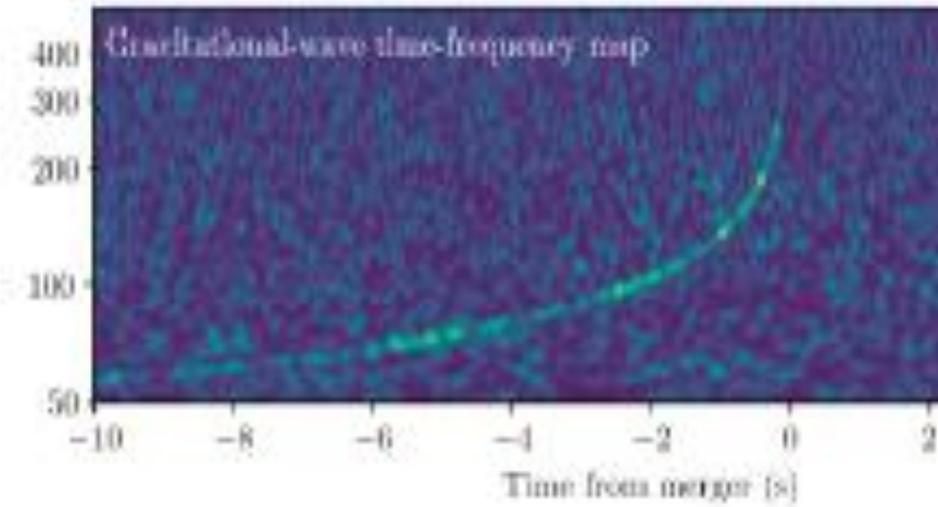
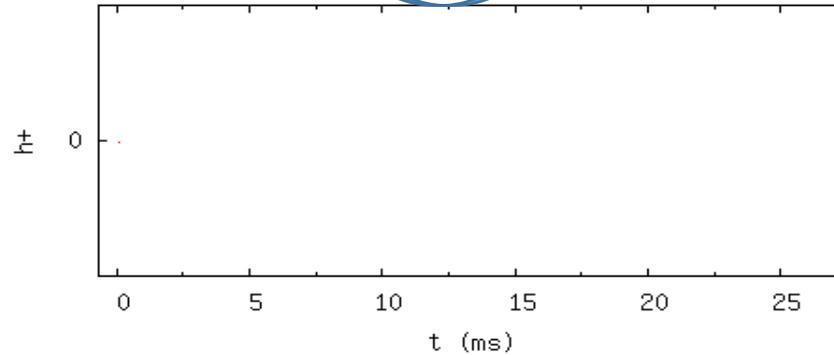


GW170817: Polarizability of neutron star (a giant nucleus)



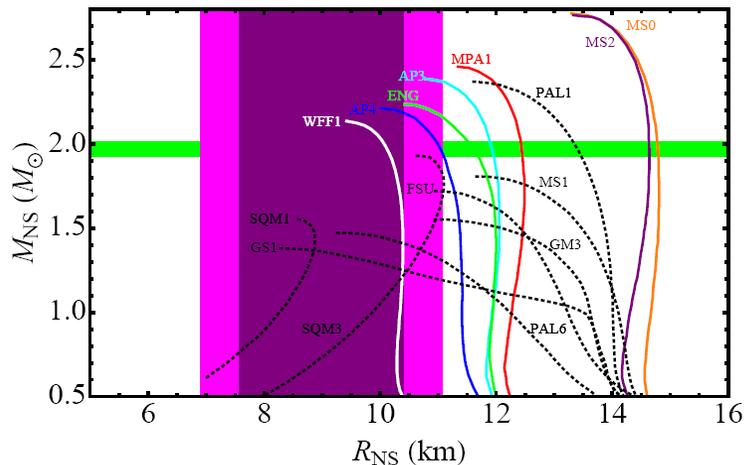
Dimensionless Tidal Deformability

$$\Lambda = \frac{2}{3} k_2 (R/M)^5 \quad \text{NS compactness}$$



$R_{\text{NS}} = 9.1^{+1.3}_{-1.5}$ km (90%-confidence)
Rutledge/Guillot, ApJ772 (2013)

GW ↔ Λ ↔ R/M ↔ EOS



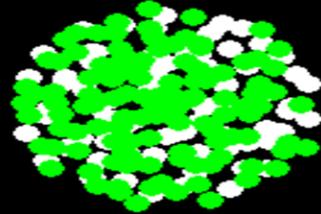
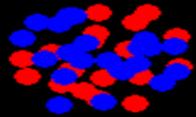
- Mass quadrupole polarizability of a NS: $\Lambda \propto R^5$
- Ligo is sensitive to the increase in orbital frequency as the system loses energy to both GW and internal excitation of NS.
- GW170817 data place limits on polarizability of NS and hence up limits on NS radius.

• Consistent, but less strictive: [arXiv:1801.04620](https://arxiv.org/abs/1801.04620)



Very Brief Rev. of $E_{\text{sym}}(\rho)$ at $\rho < \rho_0$ in HIC

```
40 18 + 197 79
E = 1164.00000
b = 1.00000
t = 0
Blue and Green are neutrons!
nrns : 1
```

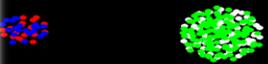


Equation of State of Asymmetric Nuclear Matter and Collisions of Neutron-Rich Nuclei

Bao-An Li,^{1,*} C. M. Ko,^{1,†} and Zhongzhou Ren^{2,‡}

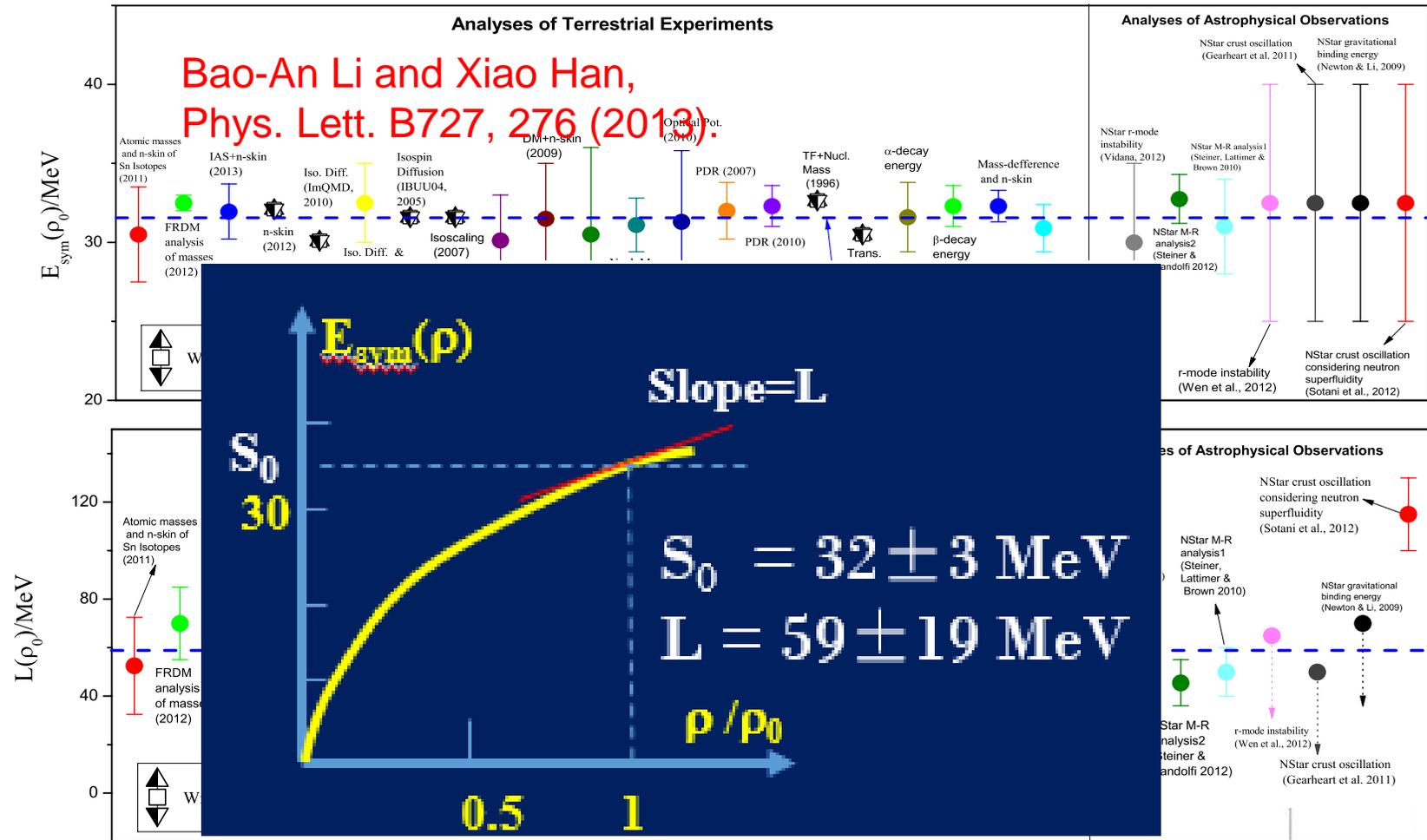
Isospin transport and the constraint of $E_{\text{sym}}(\rho)$

At sub-saturation densities

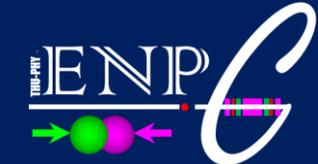


List extends:

- Isospin diffusion (MSU ...)
- Isospin scalaring and isospin fractionaiton (MSU...)
- n/p ratio of fast and pre-equilibrium nucleons (MSU ...)
- N/Z of the emitted fragments (LNS, TAMU, MSU, HIRFL ...)
- GMR strength (ND ...)
- HBT correlation function (KVI, MSU, HIRFL ...)
-



Proton radioactivity: $E_{\text{sym}} = 29.3 \text{ MeV}$ $L = 51.8 \text{ MeV}$
 N. Wan, C. Xu et al., Phys. Rev. C 94, 044322 (2016).

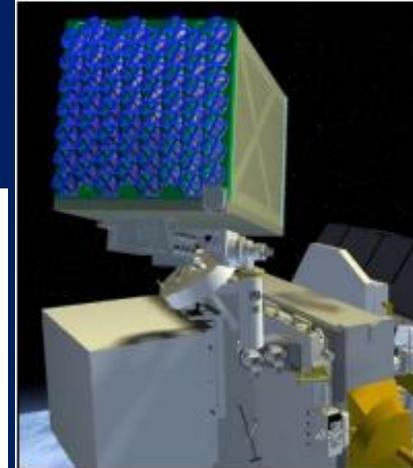
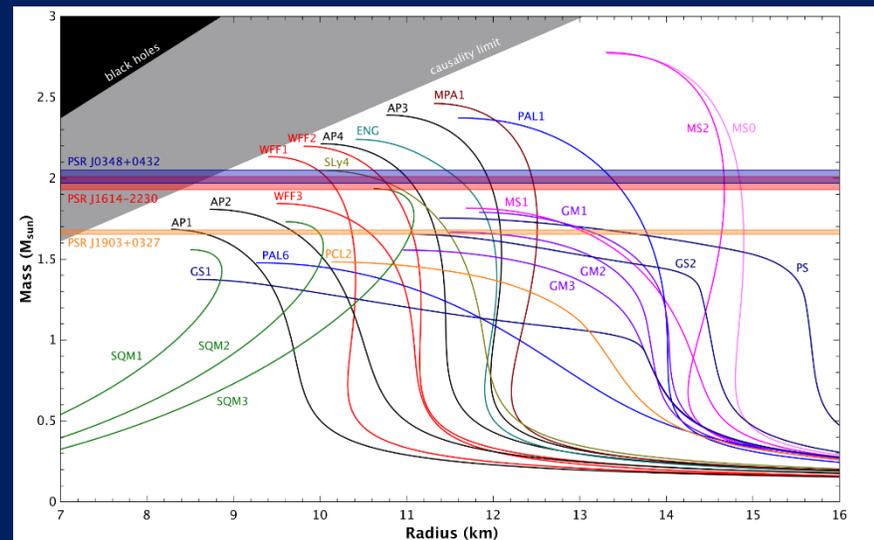


$E_{\text{sym}}(\rho)$ becomes a frontier in major Labs

Neutron Star Observatory:

The Neutron Star Interior Composition Explorer (NICER)

Key Objective: Constrain the equation of state of bulk nuclear matter through precise mass and radius measurements of several neutron stars.



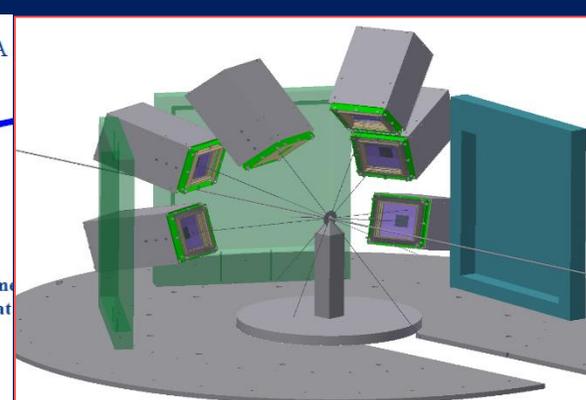
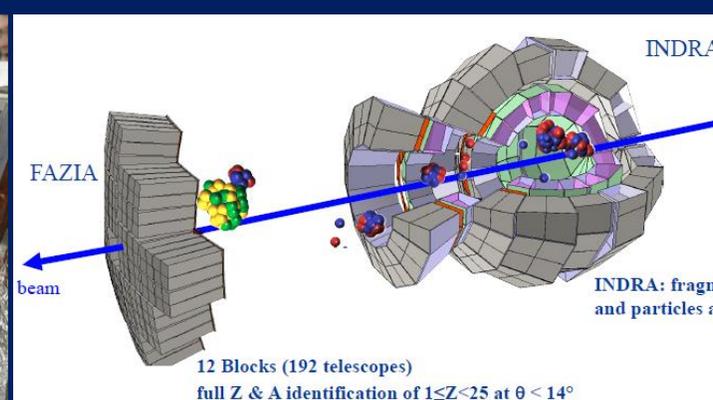
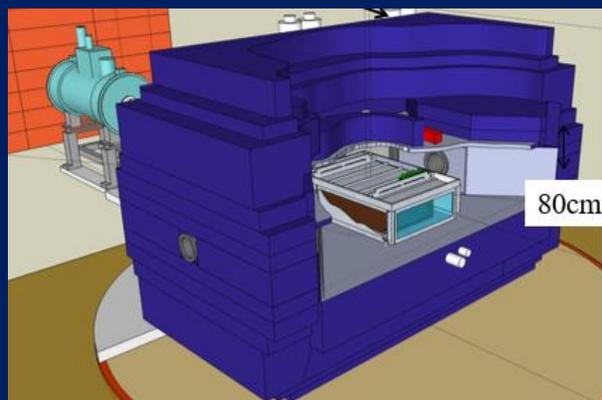
HI accelerator and RIB facilities:

SAMURAI-TPC@RIKEN

HIRA@FRIB

INDRA@GANIL

RIBLL @ HIRFL



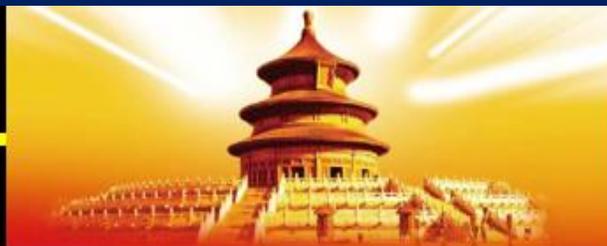
What is our Motivations ?

1) Look for new $E_{\text{sym}}(\rho)$ ($\rho < \rho_0$) probes in slow process for the enhanced sensitivity.

Neck Emission in Fission reactions: Low density neutron-rich neck, possibly a long time process.

(First presented on 8th China-Japan joint nuclear physics symposium, Oct. 2012)

The 8th China-Japan Joint Nuclear Physics Symposium



Oct. 15-19, 2012, Beijing

Fast Fission and Symmetry Energy Studies in $\text{Ar}+\text{Au}$ reactions at 35 MeV/u

Zhigang Xiao
Department of Physics, Tsinghua University

The 8th China-Japan Joint Nuclear Physics Symposium (CJJNPS 2012)
15-19 October 2012 Beijing, China



2) To develop a method to measure quantitatively the time scale of the transport of IDOF.

1 Introduction

2 Isospin transport in HIC and Isospin Chronology

2.1 Isospin dependent particle emission hierarchy (3')

2.2 Long time isospin-drift process and $E_{\text{sym}}(\rho)$ (3')

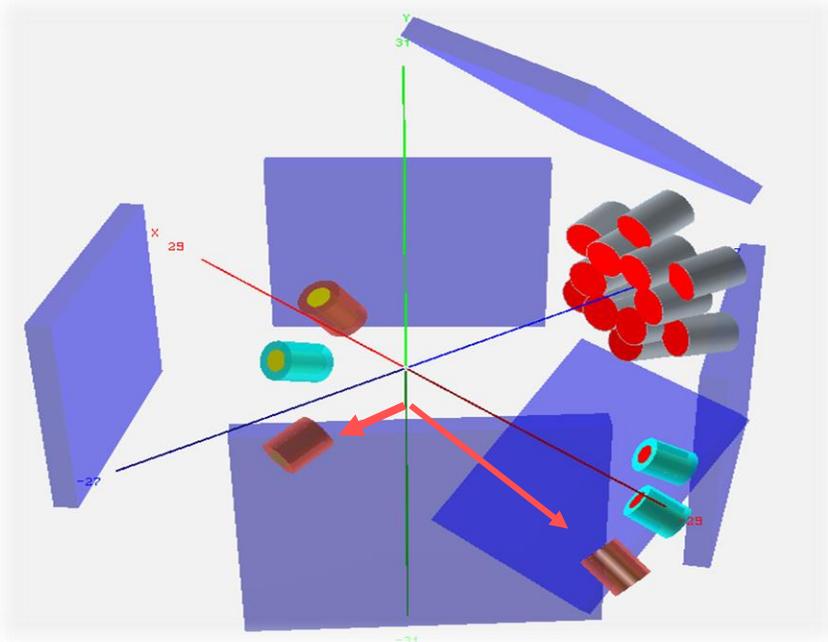
2.3 Isospin Chronology with HIRA^{TU}: future plan (4')

3 A new tool to constrain $E_{\text{sym}}(\rho)$ (2')

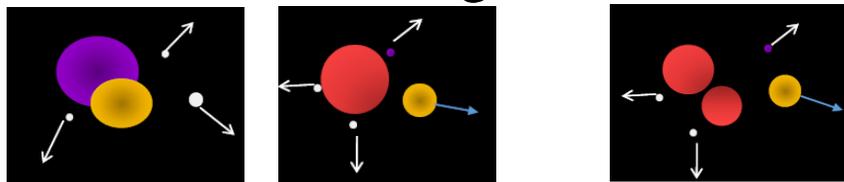
4 Summary (1)

2.1 Isopsin dependent hierarchy of particle emission

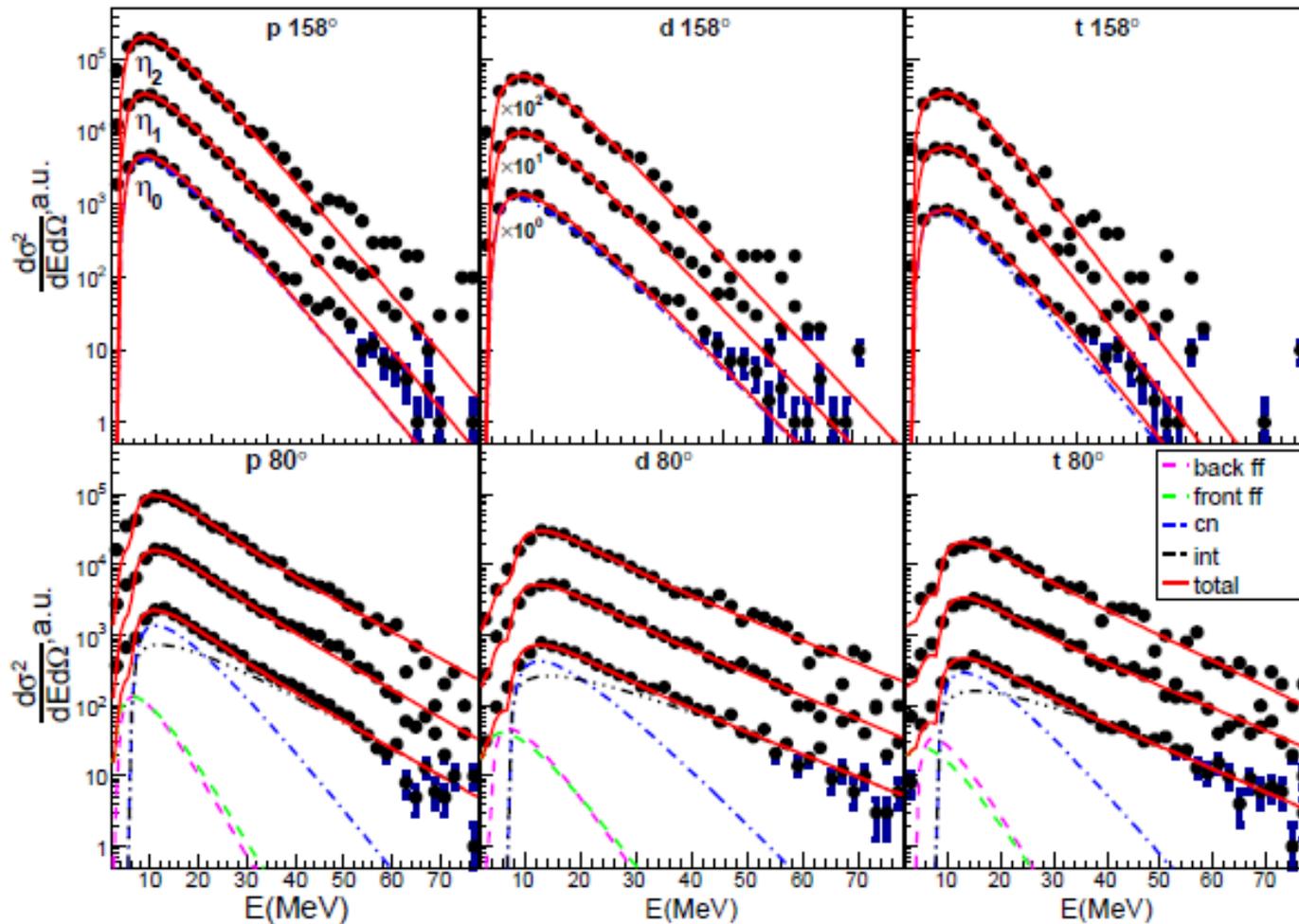
35 MeV/u Ar+ Au.
 Trigger: 2 fold fragments .AND. 1 LCP



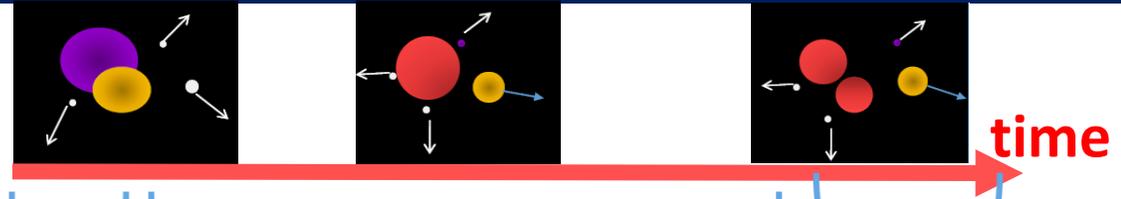
• Three Moving source:



$$\frac{d^2\sigma}{d\Omega dE} = \frac{N}{2(\pi T)^{3/2}} (E - E_c)^{1/2} \exp[-(E - E_c)/T]$$



Minimum χ^2 analysis and particle emission hierarchy



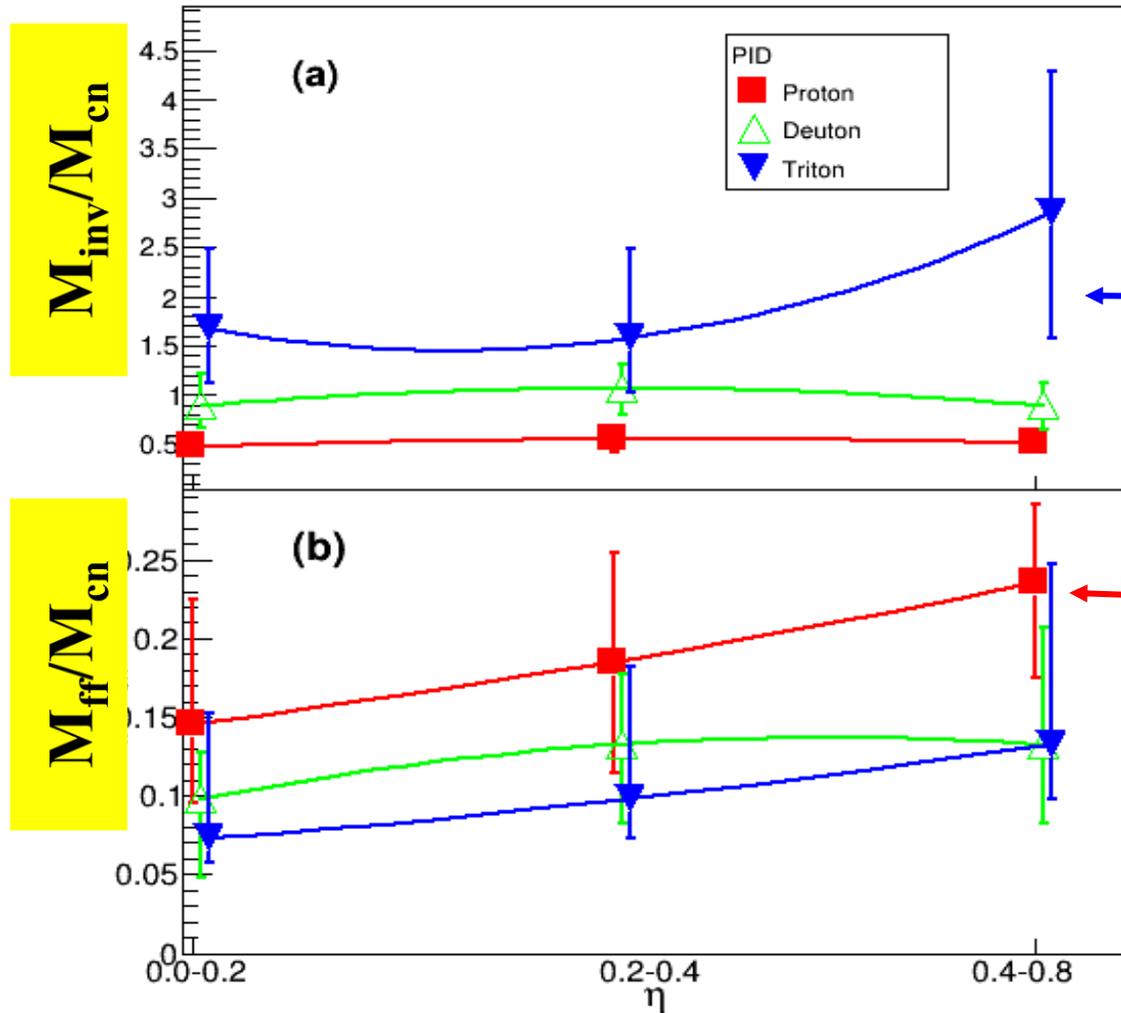
Int. Velo.

CN

FF

More triton emission

More proton emission

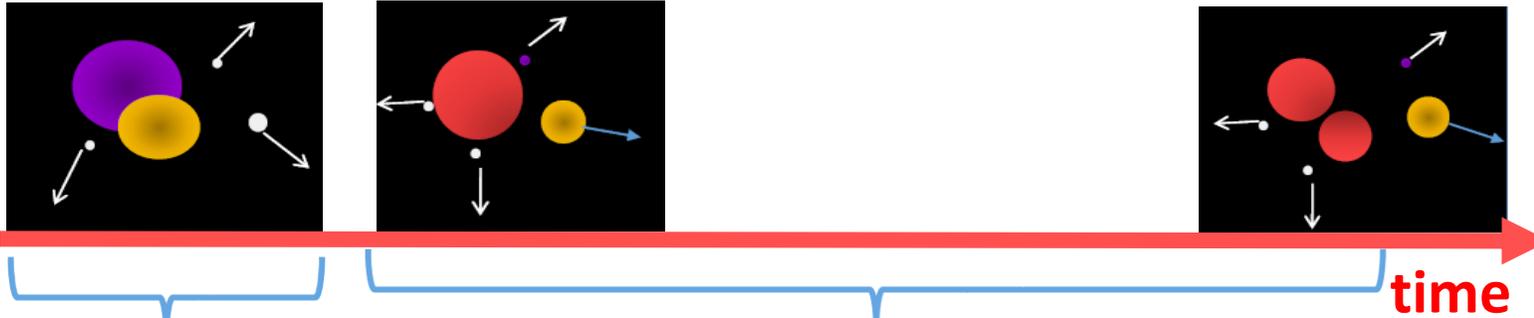


A isospin-dependent hierarchy of particle emission is observed.

R. S. Wang, Y. Zhang, XZG... et al.,
PRC89 (2014) 064613

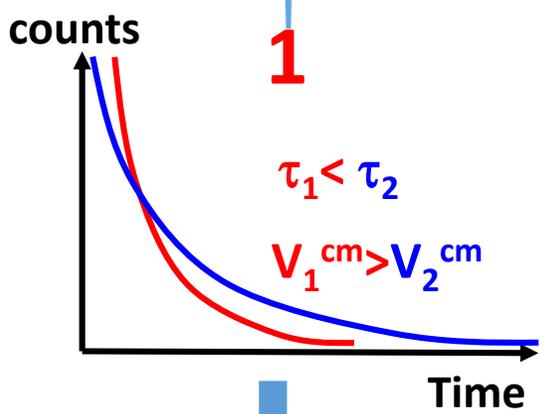


Build a qualitative relation between the angle in lab and the emission time

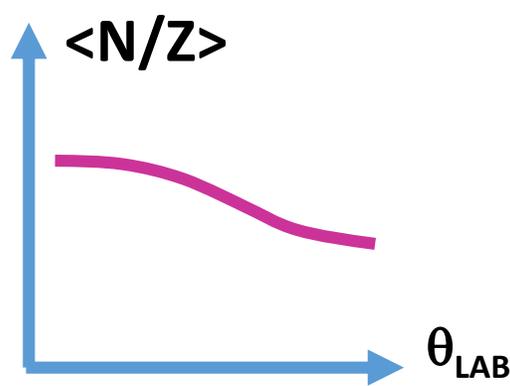
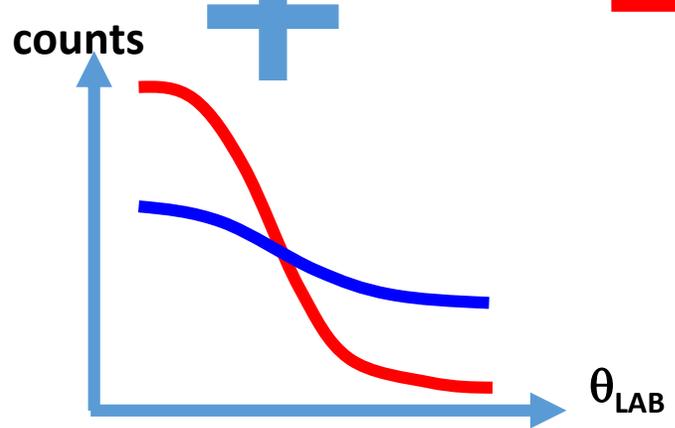
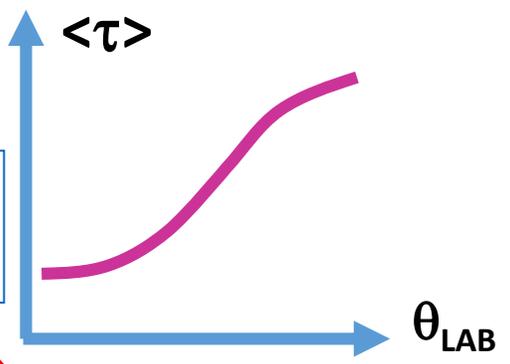


1 Angular distribution in large angular range reflects the time evolution of isospin transport;

2 A stiffer symmetry energy leads to faster isospin drift, thus to more rapidly changing in angular distribution.

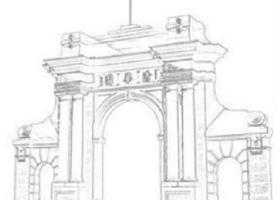


$$\langle \tau \rangle = \frac{n_1 \tau_1 + n_2 \tau_2}{n_1 + n_2}$$



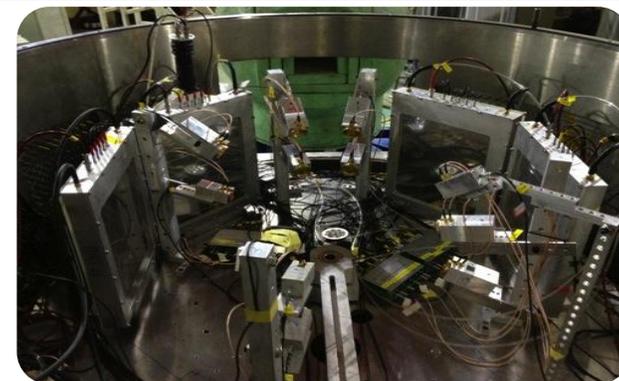
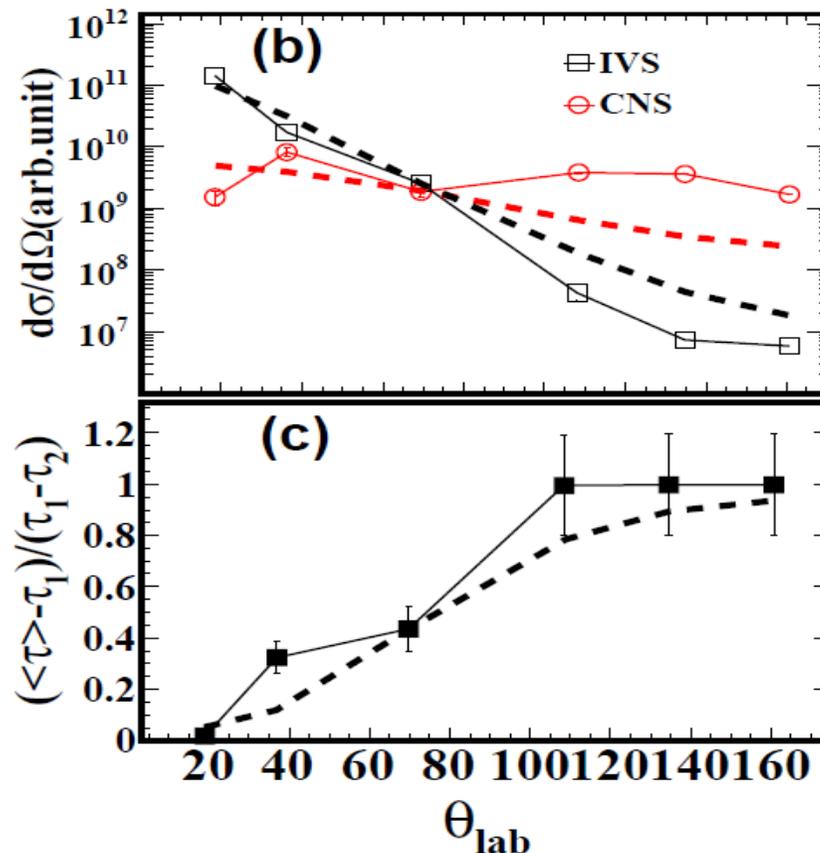
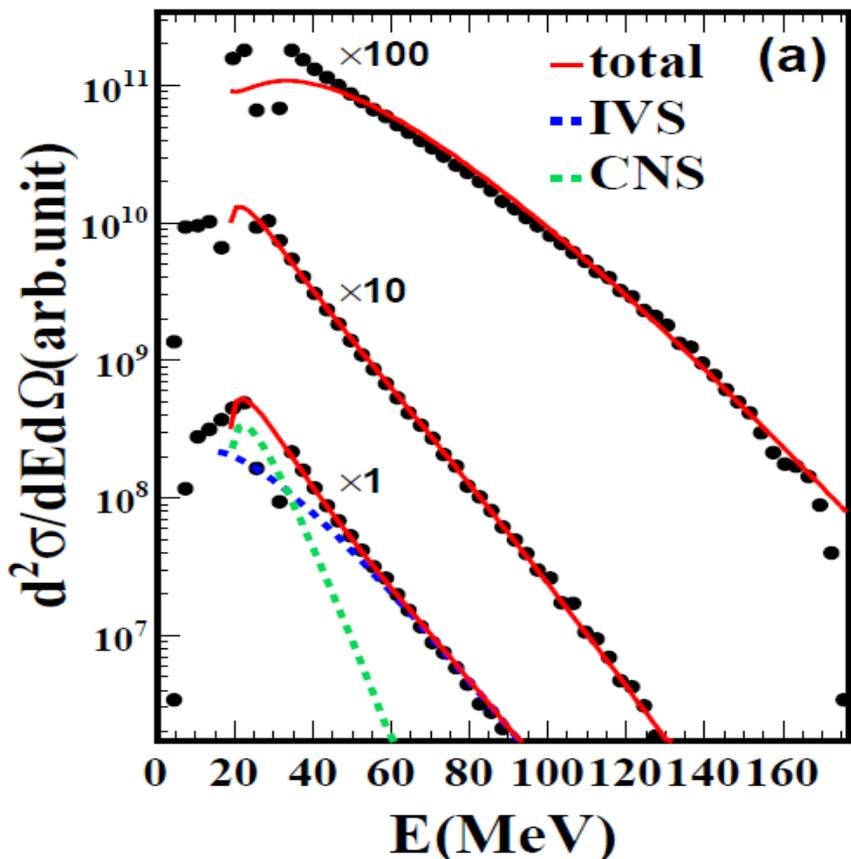
$$j_{np} = j_n - j_p = (D_n^\rho - D_p^\rho) \nabla \rho - (D_n^I - D_p^I) \nabla I$$

$$D_n^\rho - D_p^\rho \propto 4I \frac{\partial E_{sym}(\rho)}{\partial \rho}$$

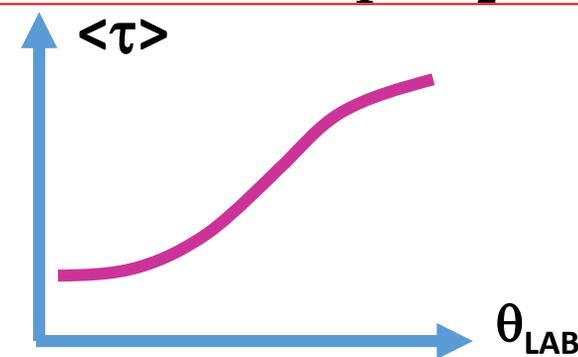


2.2 Long time isospin drift and the constraint of $E_{\text{sym}}(\rho)$

30 MeV/u Ar+Au @ RIBLL, HIRFL, Lanzhou



$$\langle \tau \rangle = \frac{n_1 \tau_1 + n_2 \tau_2}{n_1 + n_2}$$

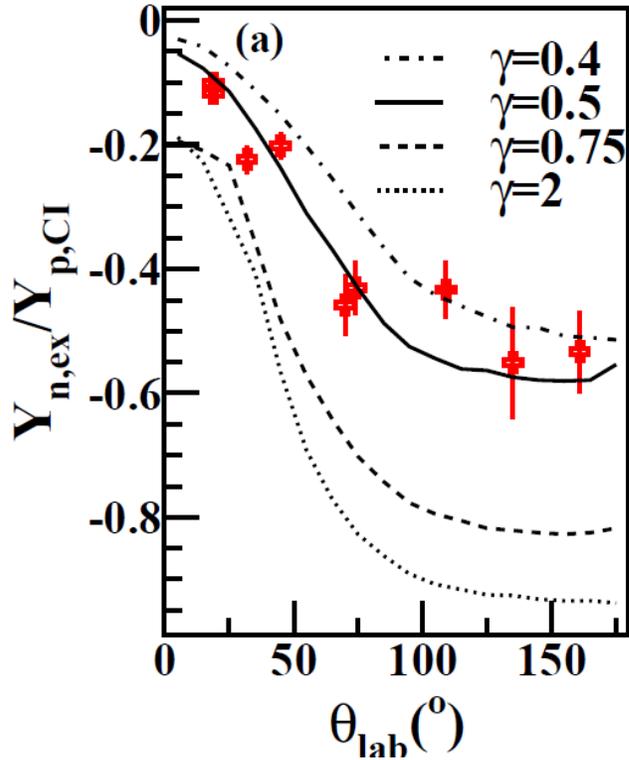


→ moving-source analysis indicates that a qualitative relation between angular distribution and the average emission time exists

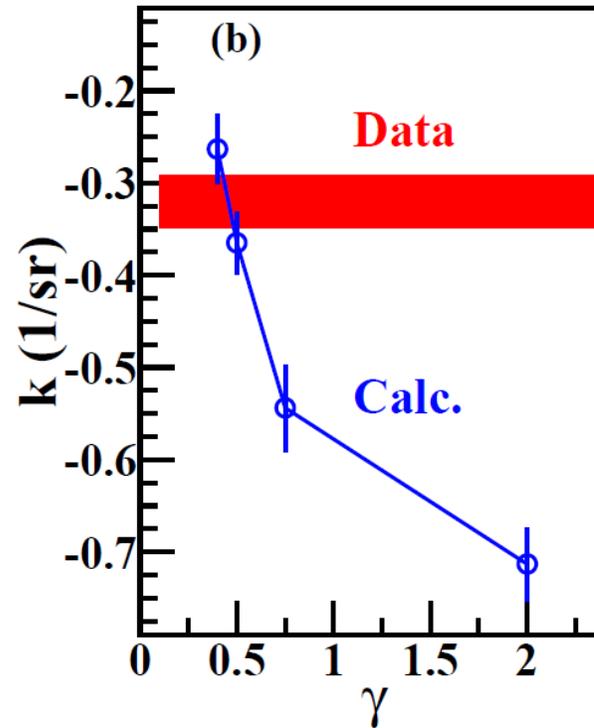
→ The relationship shall hold, even though the real process is more complex.

Constraint of the $E_{\text{sym}}(\rho)$ with IMQMD+GEMINI

$$\frac{Y_{n,\text{ex}}}{Y_{p,\text{Cl}}} = \frac{\sum y_i (N_i - Z_i)}{\sum y_i Z_i}$$



$$\frac{Y_{n,\text{ex}}}{Y_{p,\text{Cl}}} = k\theta_{\text{lab}} + b$$



1) In the wide angular range, the neutron richness decreases with angle in lab. The rapidness depends on the stiffness of $E_{\text{sym}}(\rho)$
 → Isospin drift is long time process, persisting from early dynamic emission to late statistical emission

2) $E_{\text{sym}}(\rho)$: $\gamma = 0.46 \pm 0.025$ (STDEV)
 $L = 47 \pm 14$ MeV (CL=95%)
 with S_0 fixed at 28.3 MeV.



Y. Zhang , ... ZGX , **PRC 95**, 041602(R) (2017)

RAPID COMMUNICATIONS

PHYSICAL REVIEW C 95, 041602(R) (2017)

Long-time drift of the isospin degree of freedom in heavy ion collisions

Yan Zhang (张嫣),¹ Junlong Tian (田俊龙),^{2,*} Wenjing Cheng (程文静),¹ Fenhai Guan (关分海),¹ Yan Huang (黄彦),¹

C. Xu et al, **PRC 82**, 054607 (2010).

N. Wan et al., **PRC 94**, 044322 (2016).

2.3 Isospin Chronology



- **How long is long? How short is short?**

- A chronology is an account or record of the times and the order in which a series of past events took place.

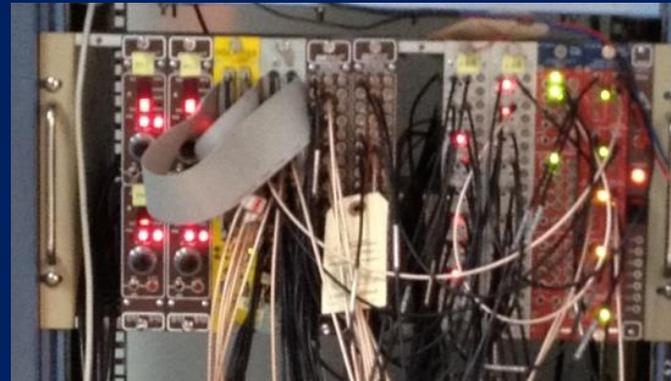
In Physics: Dynamics describes how a system/quantity evolves with time, thus time information is a basic parameter for any physical process.



10^{-2} s

10^{-8} s

10^{-21} s



$\tau \sim 10^{-21}$ s

Hanbury Brown-Twiss Method

- 1950s, Hanbury Brown and Twiss propose an intensity interferometry to measure the size information of the stellar object.

Hanbury Brown and Twiss, *Nature* **177**, 27 (1956)
 Hanbury Brown and Twiss, *Nature* **178**, 1046 (1956)

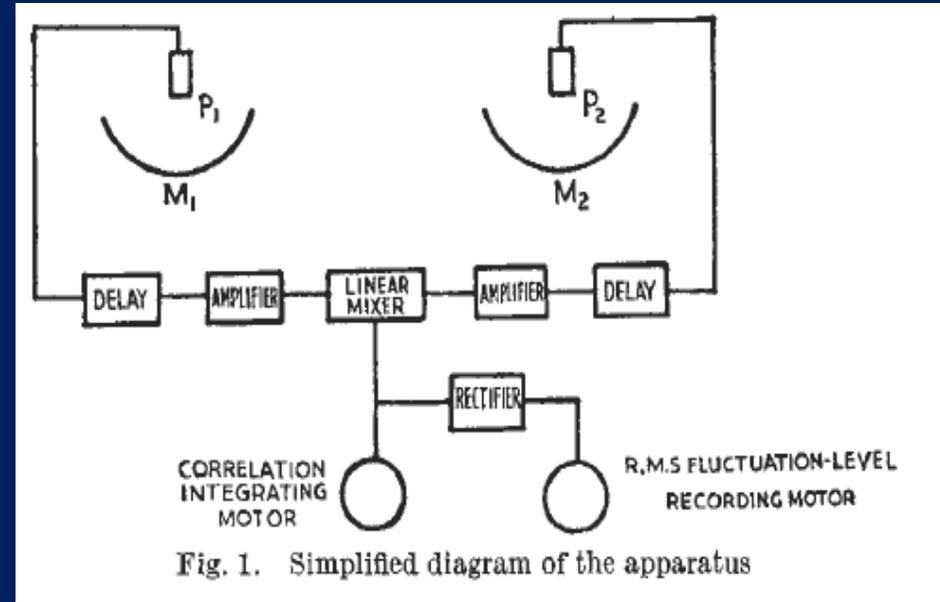
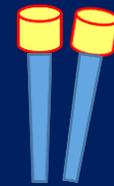
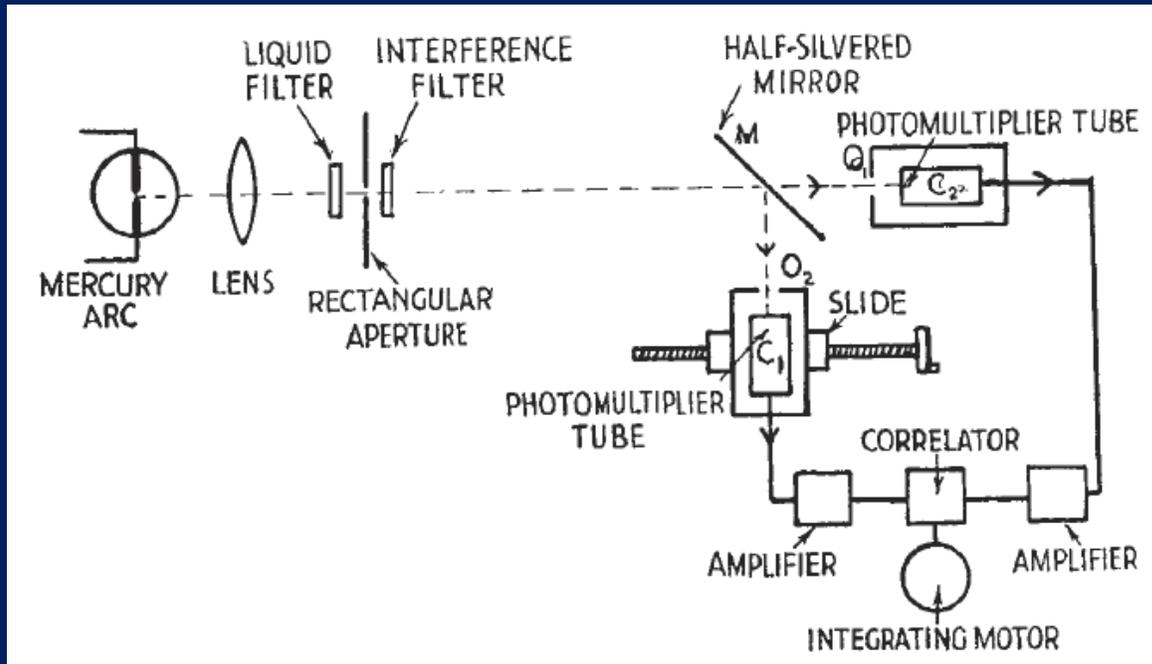
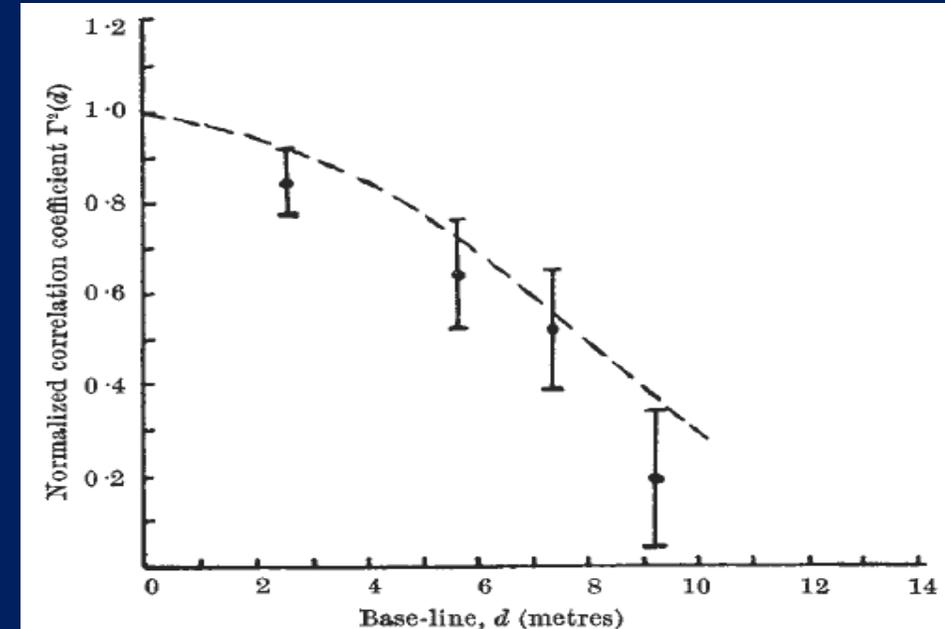


Fig. 1. Simplified diagram of the apparatus

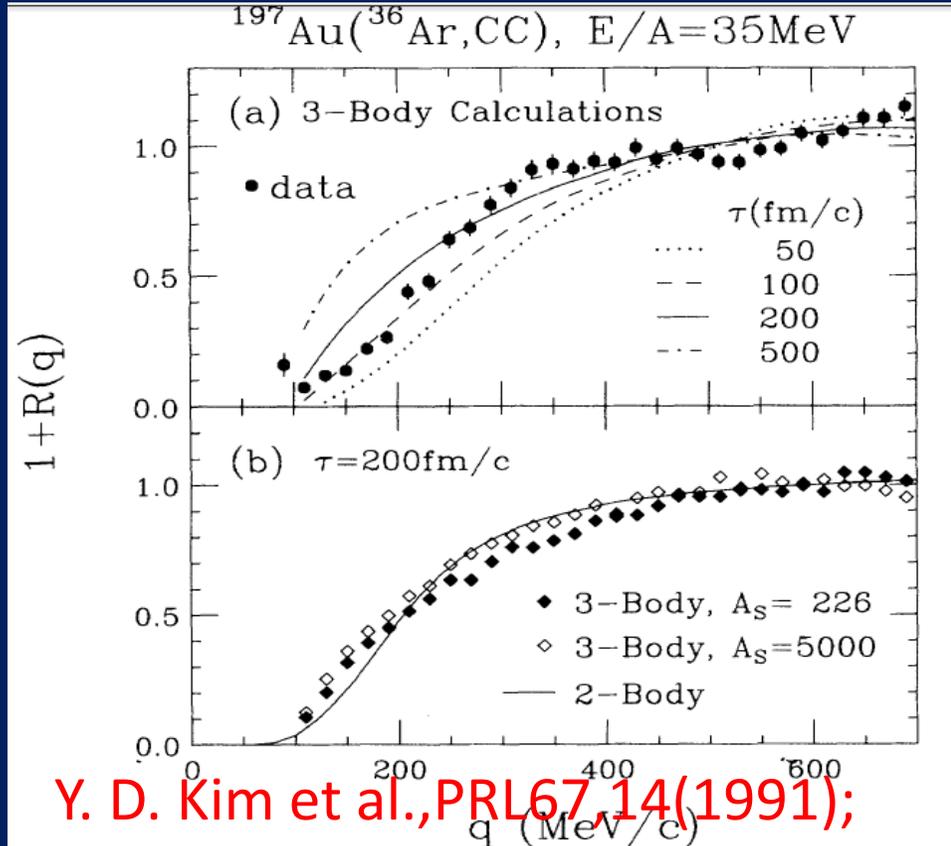


- HBT is invented to measure the space information. It turns that both space and time information are incorporated.

HBT in nuclear reactions

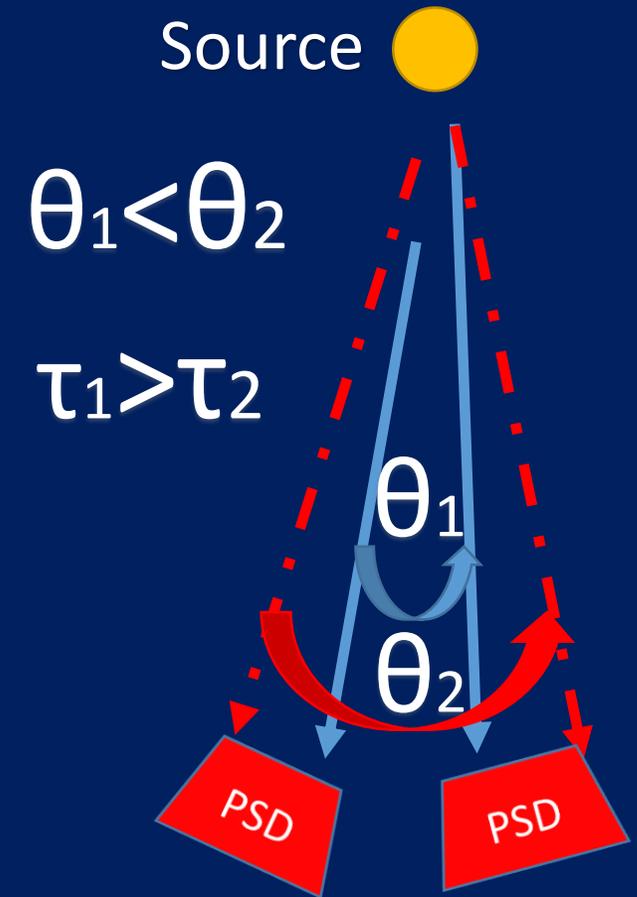
PLB70,43(1977), PRL67,14(1991); PRC51,1280(1995);
PRC,69,031605R(2004); NPA620,214(1997); PRL 77,4508(1997);
PRL70, 3534 (1993).....

$$1 + R(\vec{q}) = C \frac{P(\vec{v}_1, \vec{v}_2)}{P(\vec{v}_1)P(\vec{v}_2)}$$

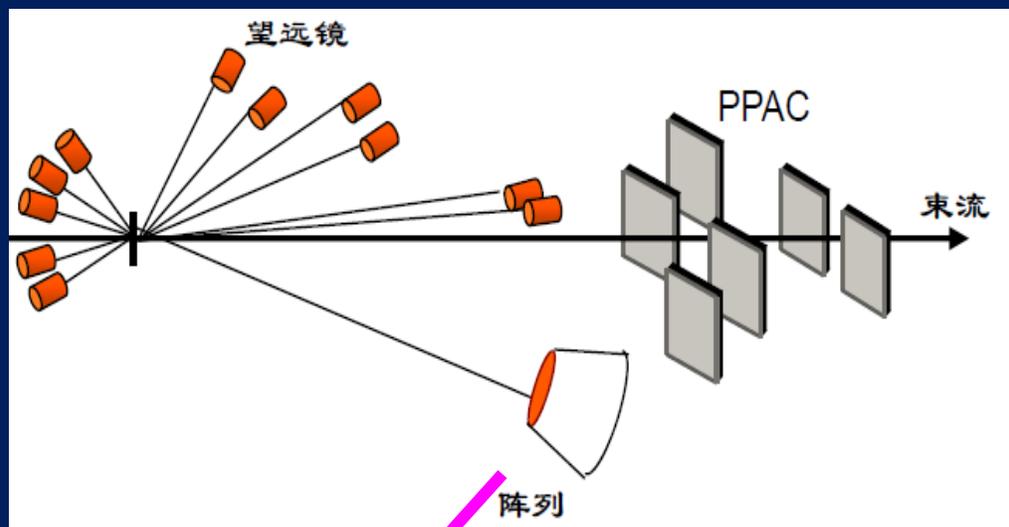


Recent application of HBT on two-proton emission mechanism

Cf YG Ma's talk

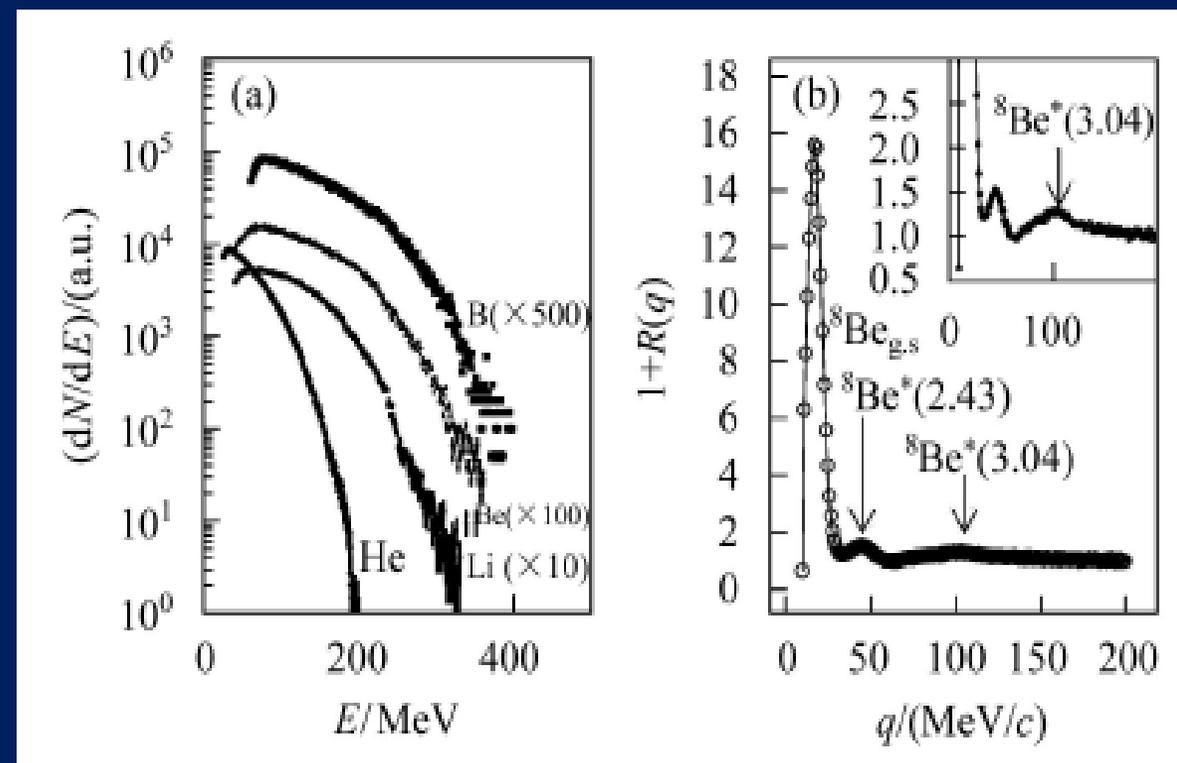
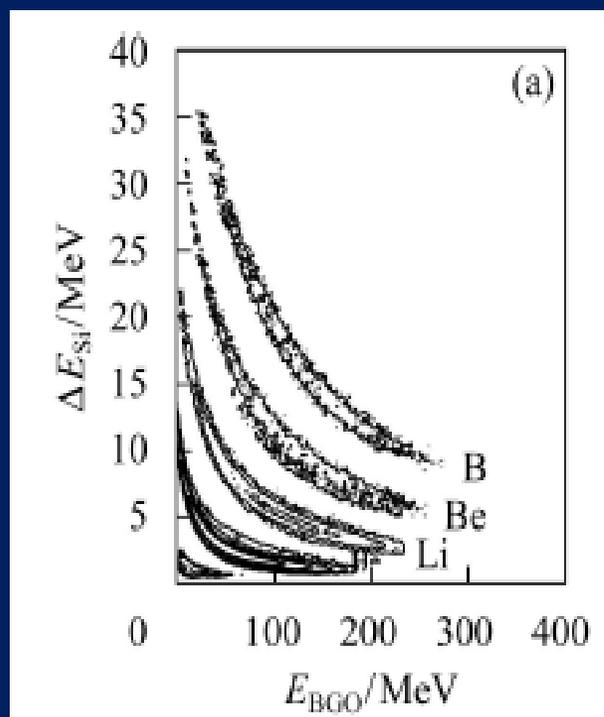
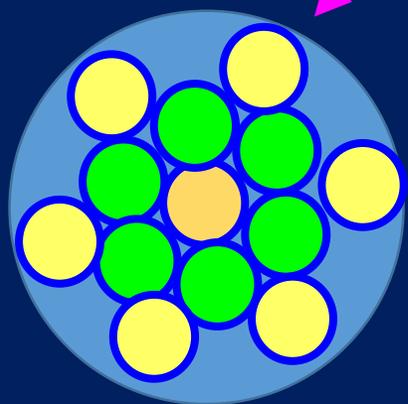


Experimental measurement of Isospin effect on IMF HBT correlation

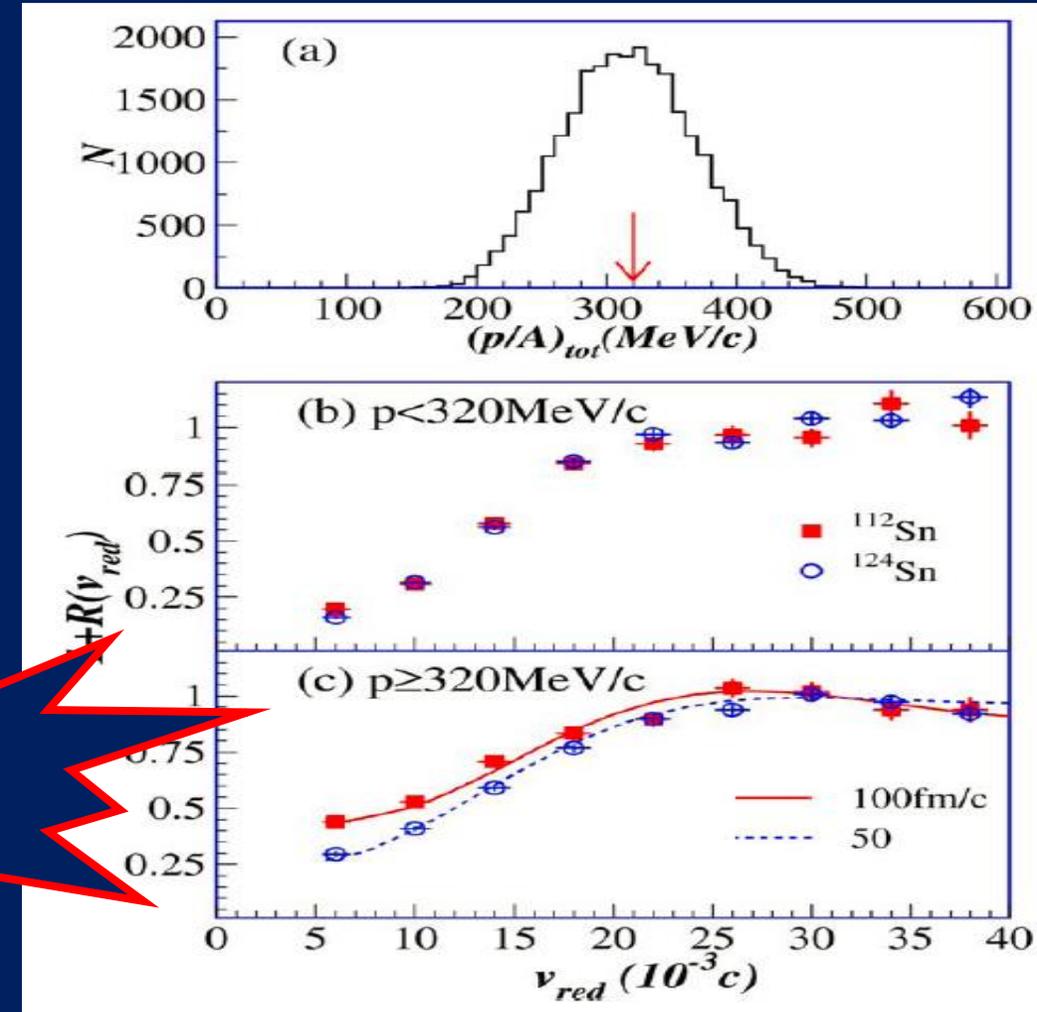
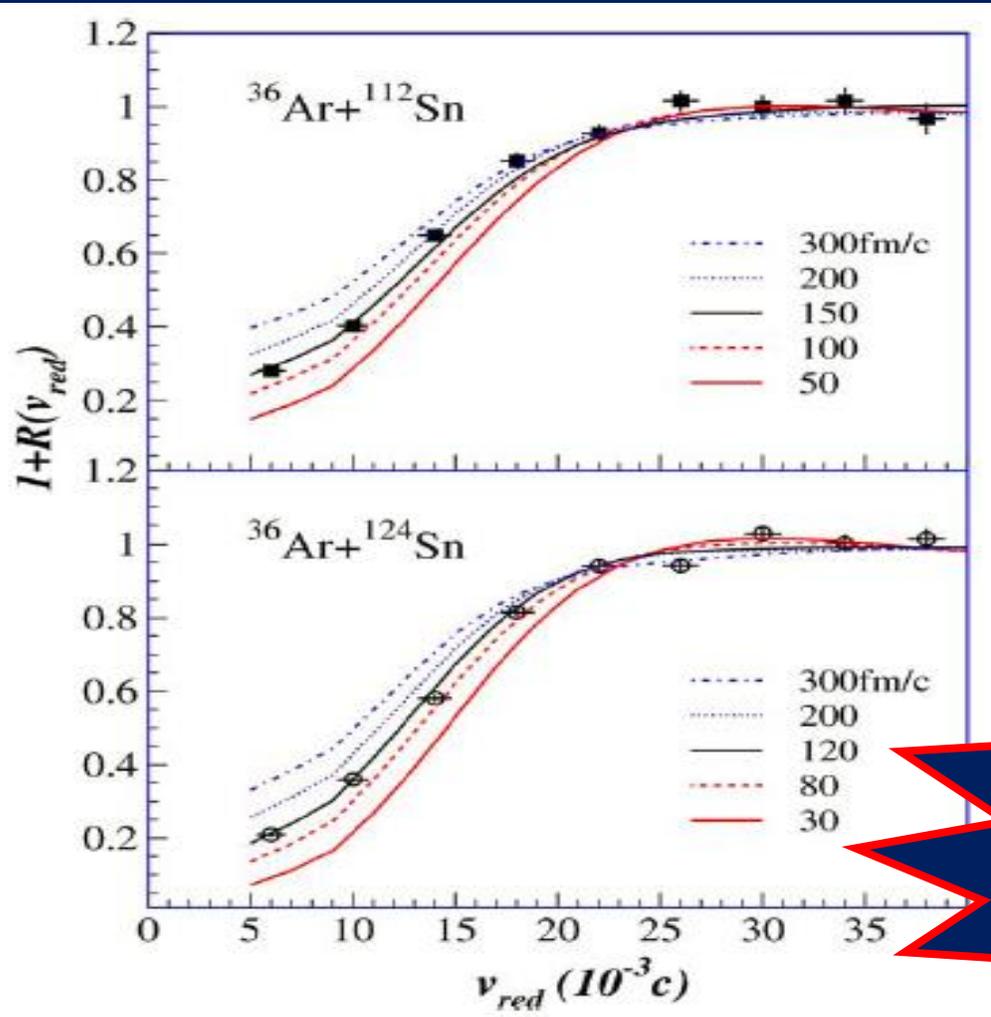


- Reaction: $35\text{MeV } ^{36}\text{Ar} + ^{112,124}\text{Sn}$
- Isospin effect on IMF HBT correlation
- Hodoscope : 13-unit closely packed Si-BGO array

Hit position Resolution $\sim 1\text{cm}$



Experimental measurement of isospin dependent HBT correlation of IMF



~50 fm/c time resolution achievable

ZGX, R. J. Hu, H. Y. Wu et al., **PLB 639**,436 (2006) ;

R. J. Hu, ZGX et al., **HEPNP 31**, 350 (2007)

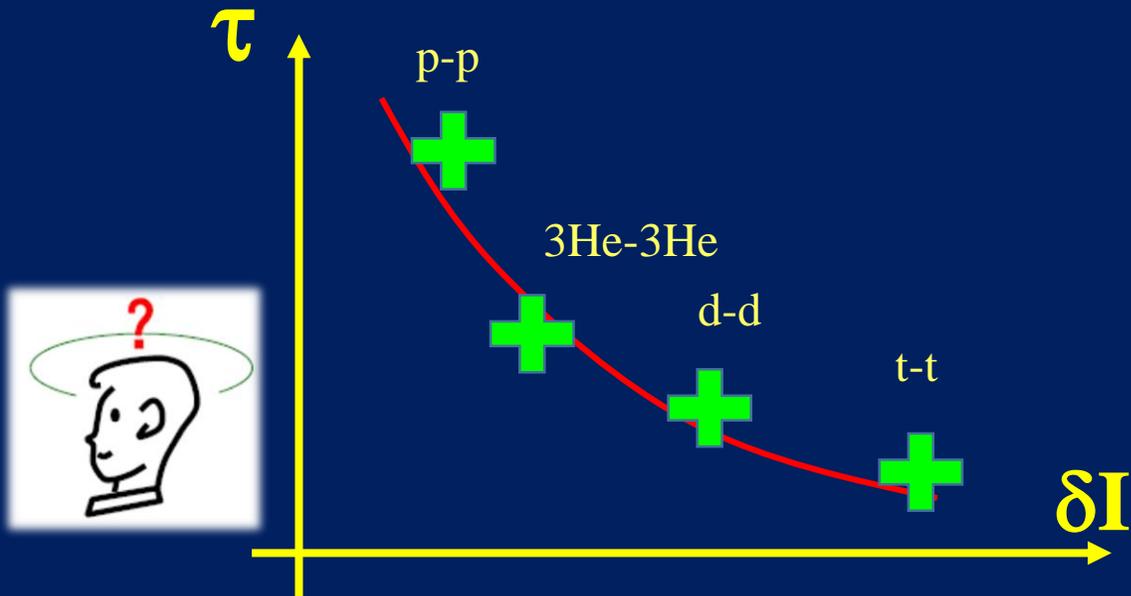
- Stronger Coulomb anti-correlation is observed in $\text{Ar} + ^{124}\text{Sn}$, this difference arises from the isospin difference of the two system.

HIRA^{TU} : A future array for Isospin chronology in HIC

- **H**heavy **I**on **R**esearch **A**rray at **T**singhua **U**niversity (**HIRA^{TU}**)
- Next Step: Isospin dependent of the particle emission time scale with HBT method.

Build a HIRA-type arrays + PPACs

First Physical goal: Isospin-resolved HBT

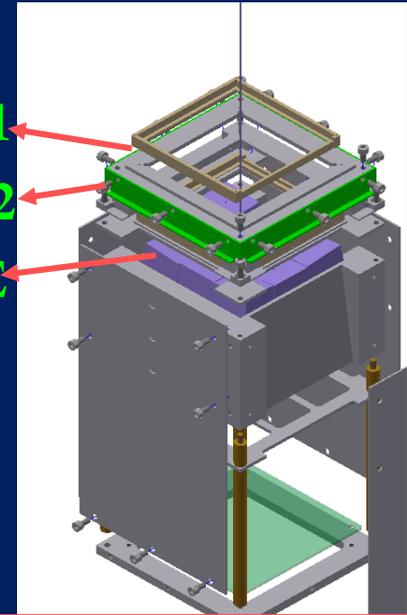


SSD - $\Delta E1$

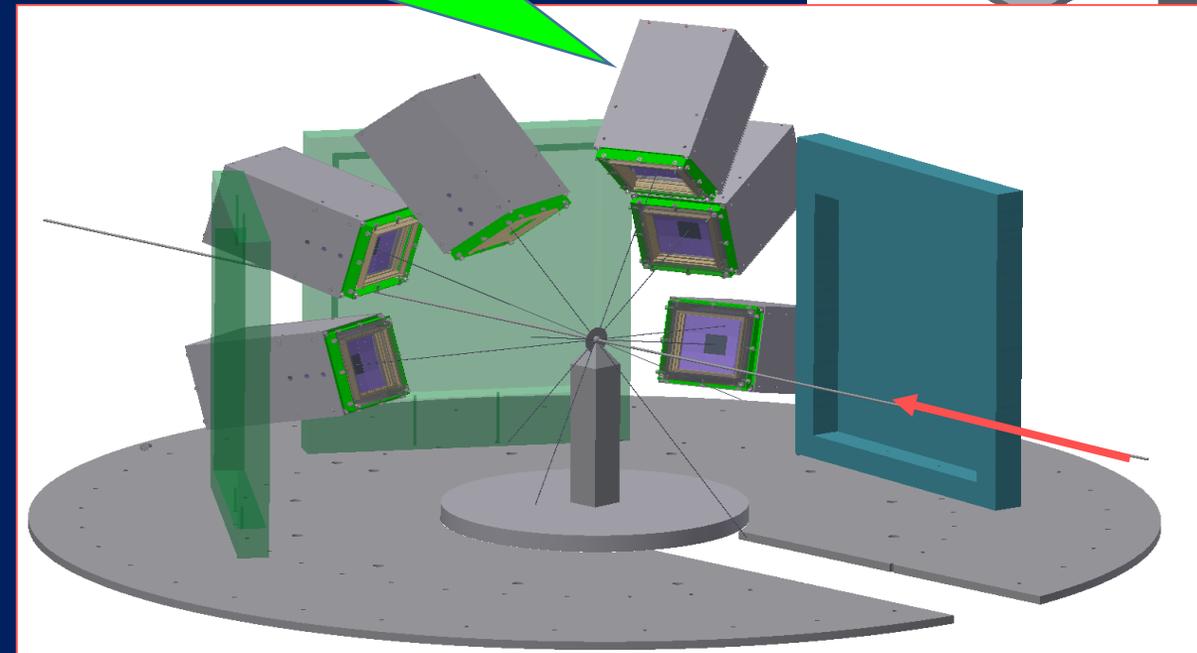
SSD - $\Delta E2$

CsI - E

Hit position Resolution $\sim 2\text{mm}$



HIRA type Telescope



HIRA^{TU}: Phase-1 Experiment

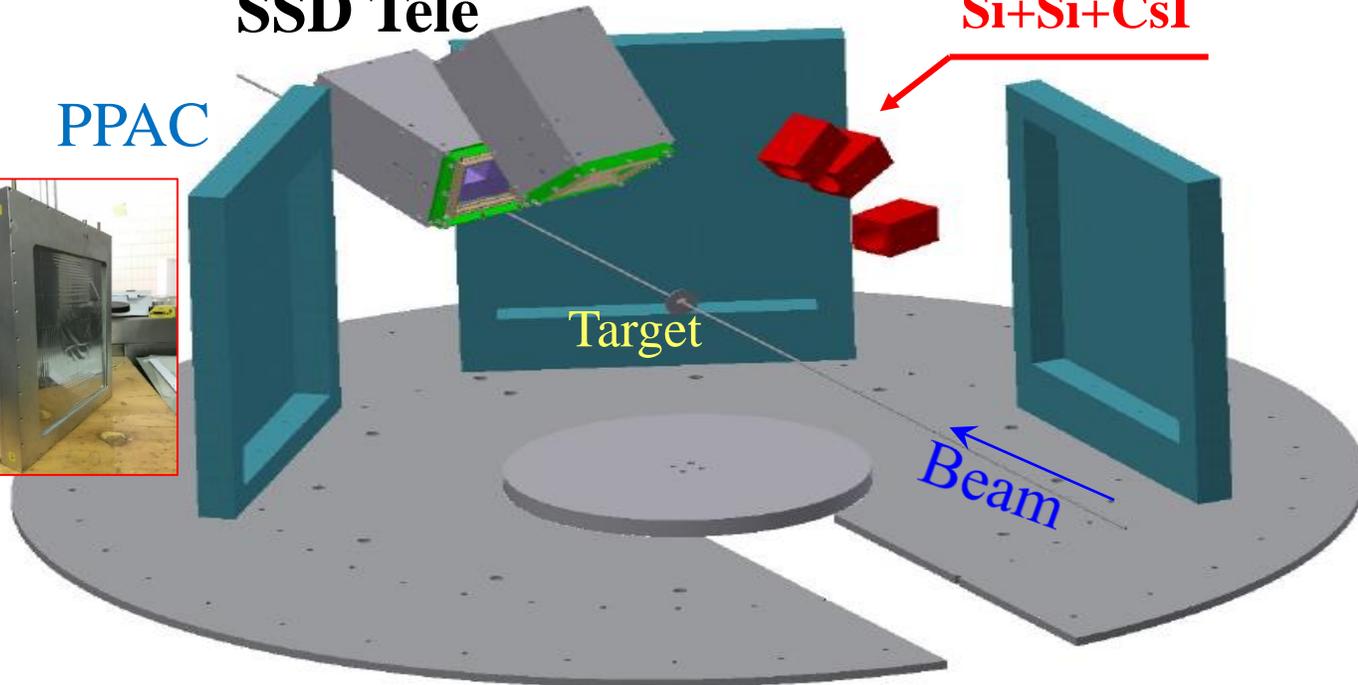
- 3 PPAC (250 mm × 350 mm) ✓
- 2 SSD-telescopes (65 μm + 1500 μm + CsI) ✓
- 3 Si(Au)-CsI Telescopes (50 μm + 300 μm + CsI) ✓



SSD Tele

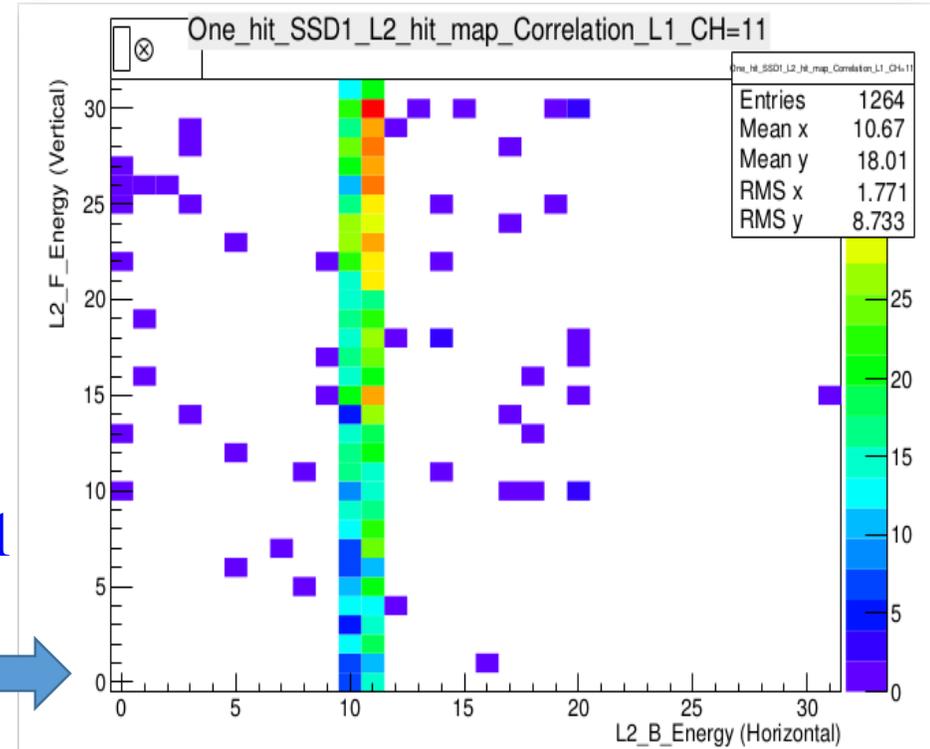
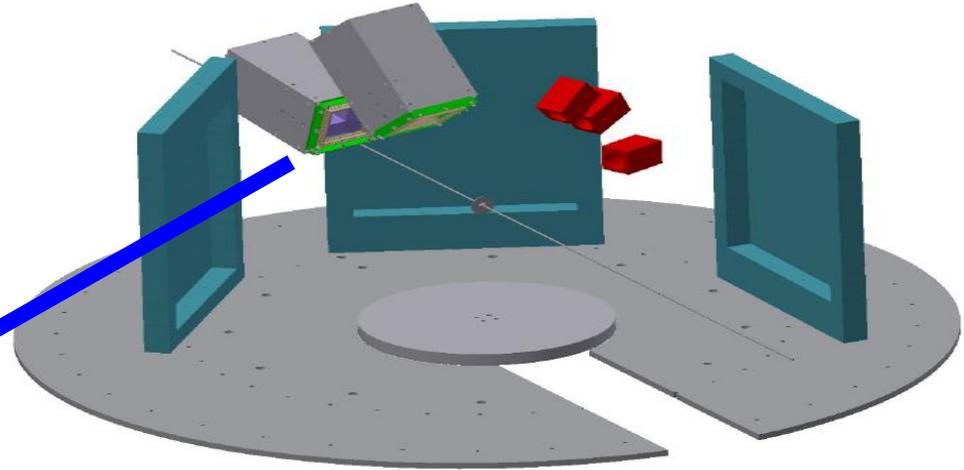
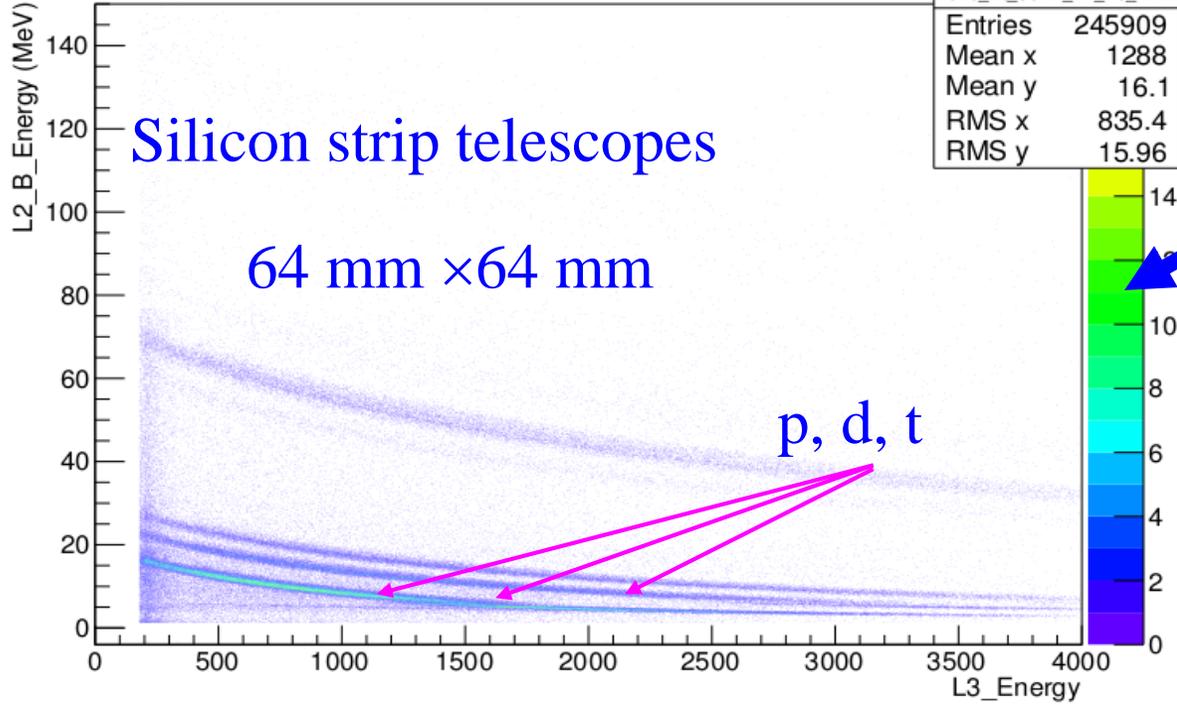
Si+Si+CsI

PPAC



one LCP in coincidence with Fission

One_hit_SSD1_E2_E3_PID

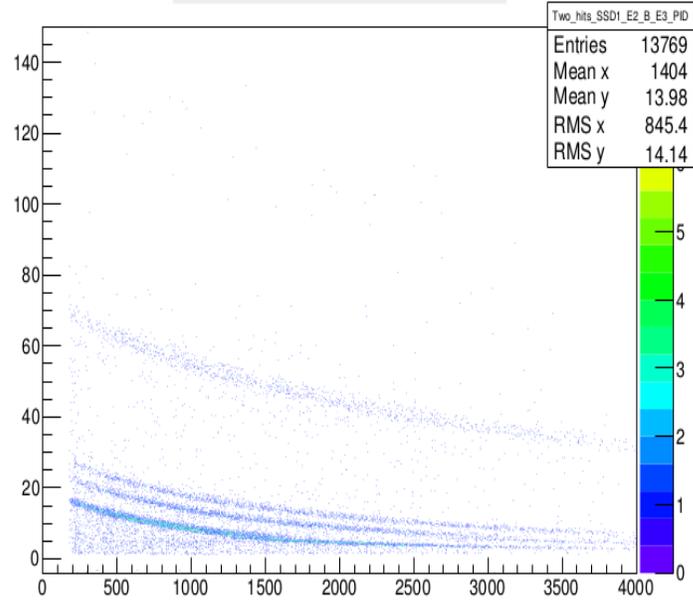


>98% matching efficiency of Layer 1 and Layer 2 of the SSD

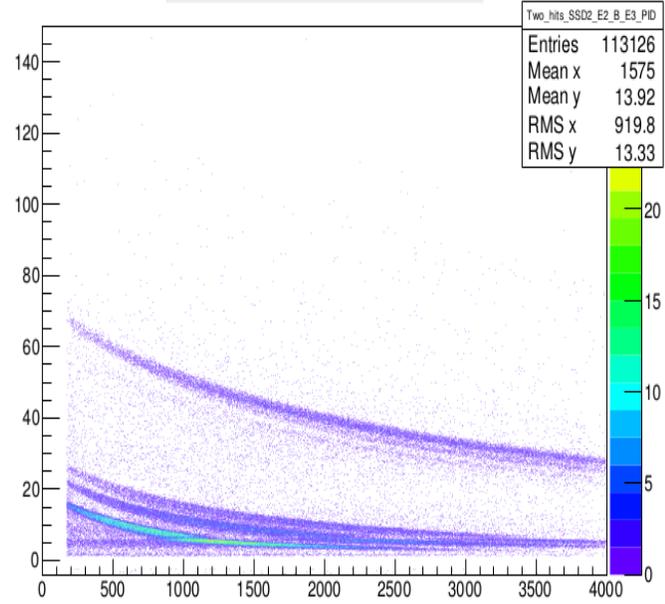


LCP-LCP correlation identified

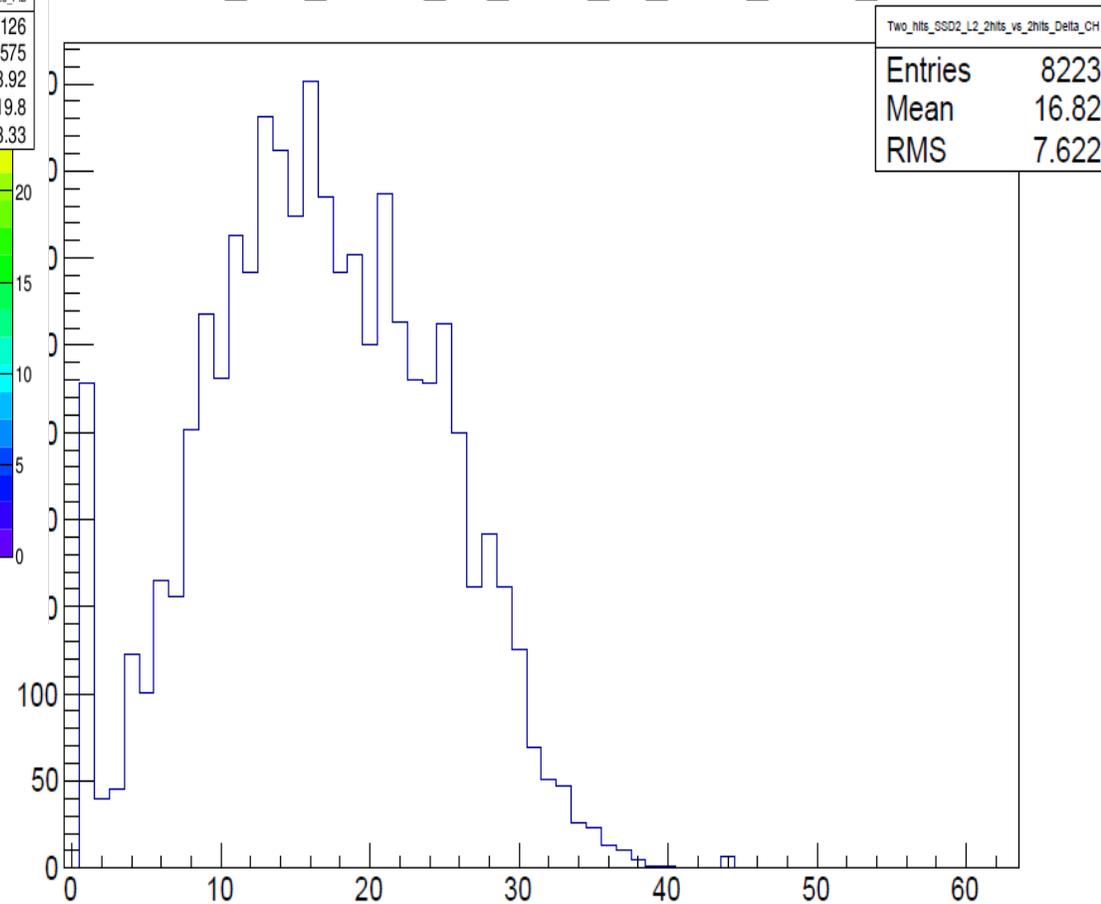
Two_hits_SSD1_E2_B_E3_PID



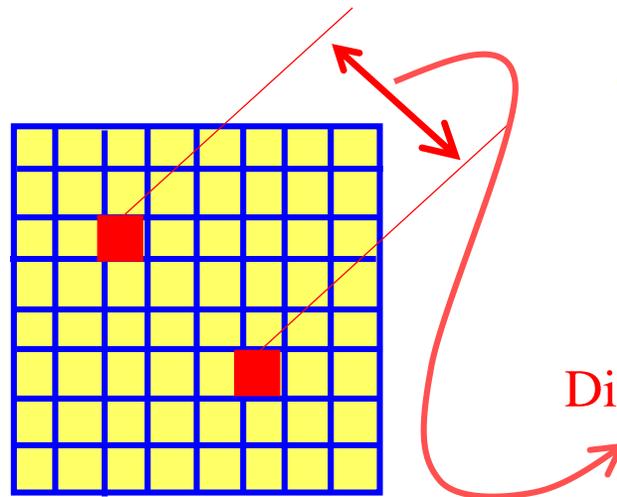
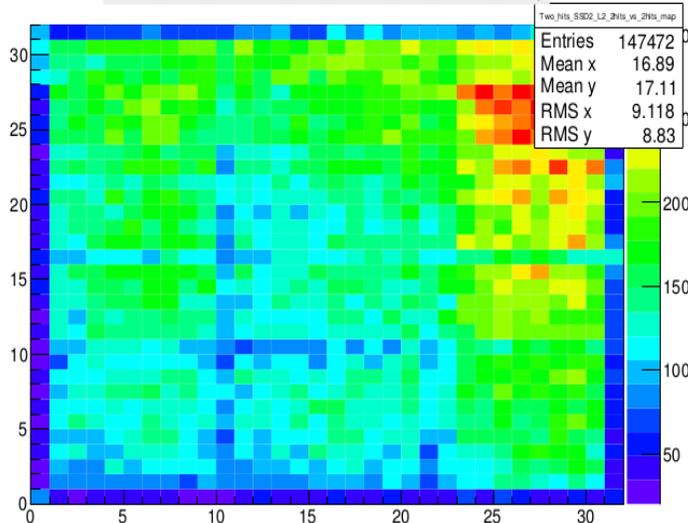
Two_hits_SSD2_E2_B_E3_PID



Two_hits_SSD2_L2_2hits_vs_2hits_Delta_CH

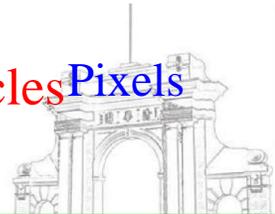


Two_hits_SSD2_L2_2hits_vs_2hits_map

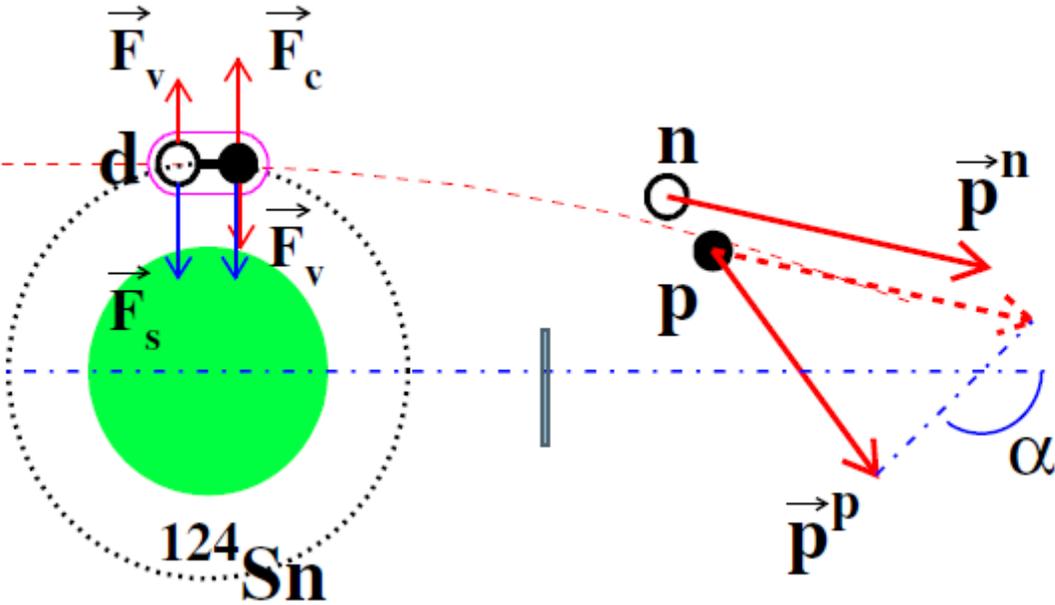


Distance between two correlated particles **Pixels**

Physical output is expected in near future!

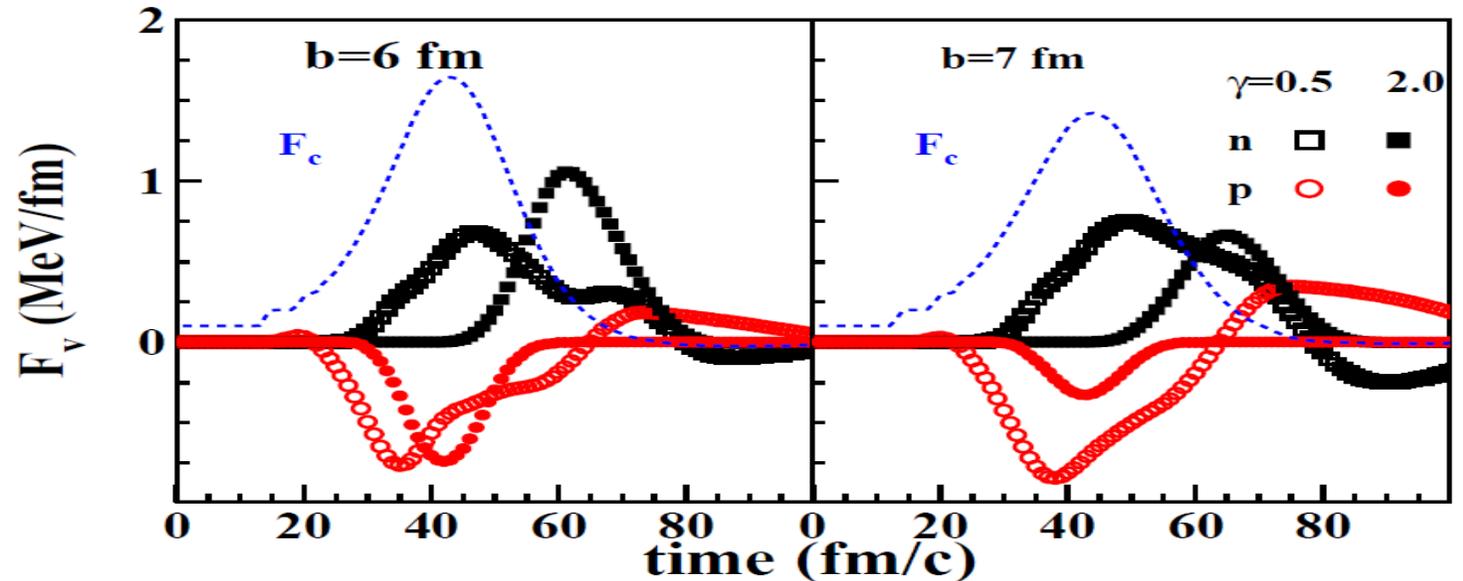


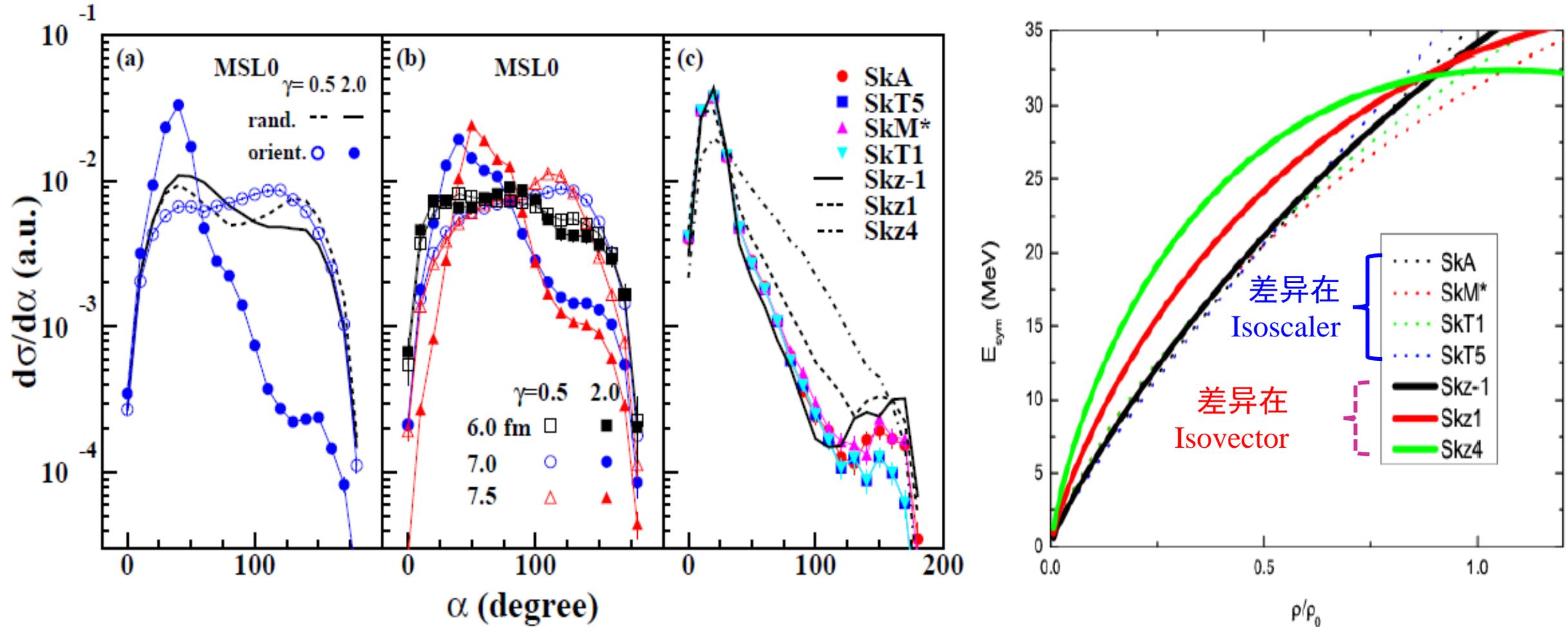
3 Isovector orientation of deuteron scattering off a target



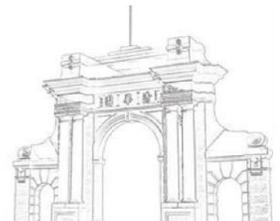
Coulomb force, 1 for proton and 0 for neutron, leads to *Coulomb polarization* (reorientation), characterized by **the moving away of proton**.

Isovector force, attractive for proton and repulsive for neutron, leads to *isovector reorientation*, characterized by **the modification of the direction of the relative motion**.

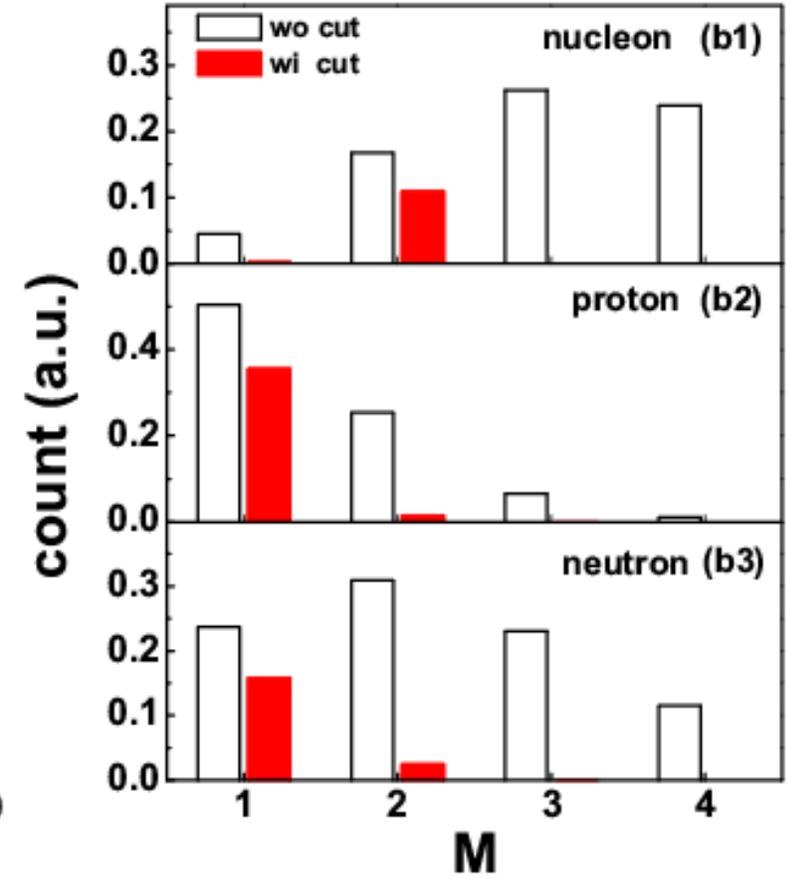
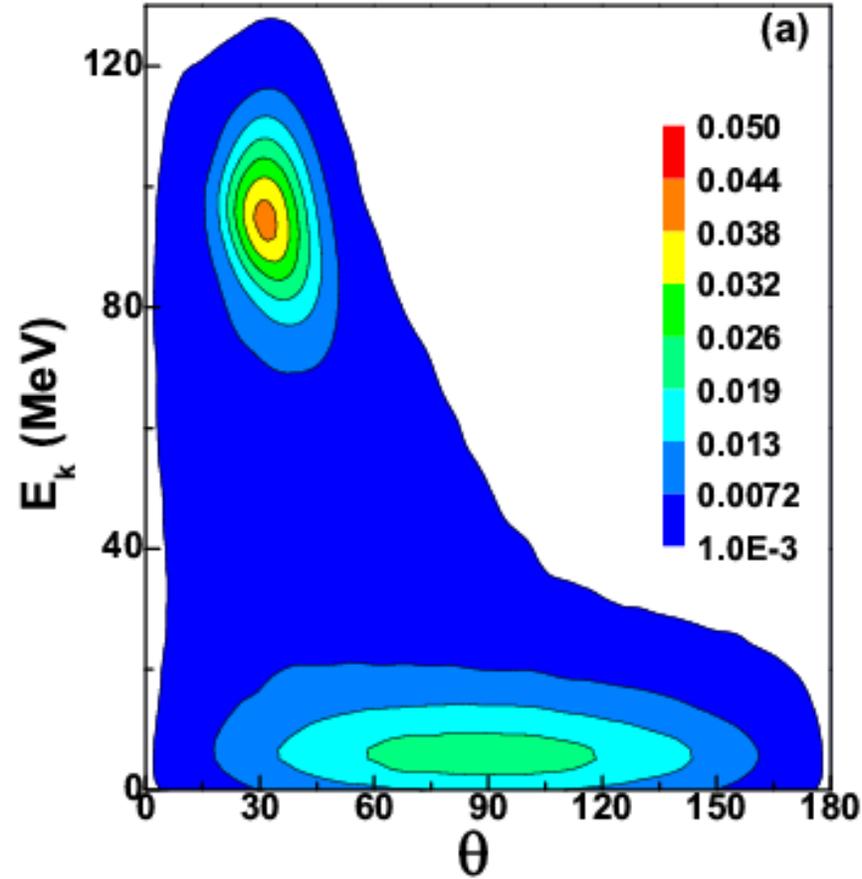
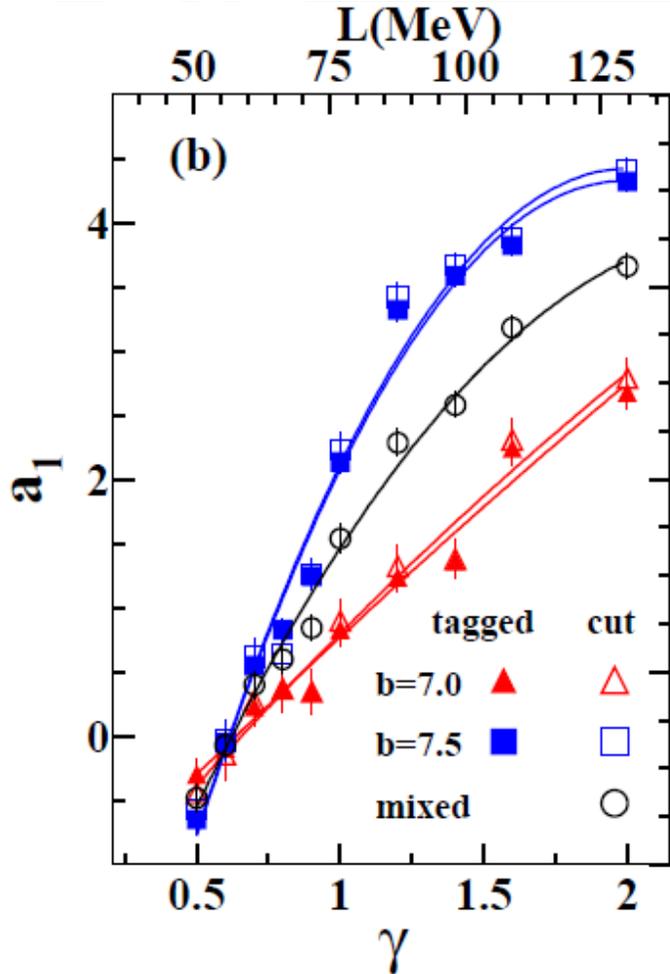




- Li Ou, [ZGX](#), Han Yi, Ning Wang, Min Liu and Junlong Tian, **PRL 115**, 212501, (2015)



Extraction from the slope of the angular distribution



- A new way to study the symmetry energy!
- It is equivalent to measure the proton- and neutron- nucleus optic potential.





4. Summary

Wealthy information of the transport of isospin degree of freedom and nEOS is contained in heavy ion collisions.

- 1) The isospin-dependent **emission hierarchy** of light charged particles has been observed, showing neutron-rich LCPs are emitted earlier.
- 2) Angular distribution of the relative neutron richness of the LCPs imply the **long time feature of isospin drift**, and set a constraint on $E_{\text{sym}}(\rho)$ with $L=33-61$ MeV at $S_0=28.3$ MeV (CL=95%)
- 3) HBT function of LCPs shows dependence on the system N/Z. Isospin chronology using HBT method is expected with **HIRA^{TU}**.
- 4) Isovector orientation effect may serve as a novel tool to study the nuclear EOS.

*Happy Birthday to Prof. Akito Arima
Much peace, happiness and good health to you*

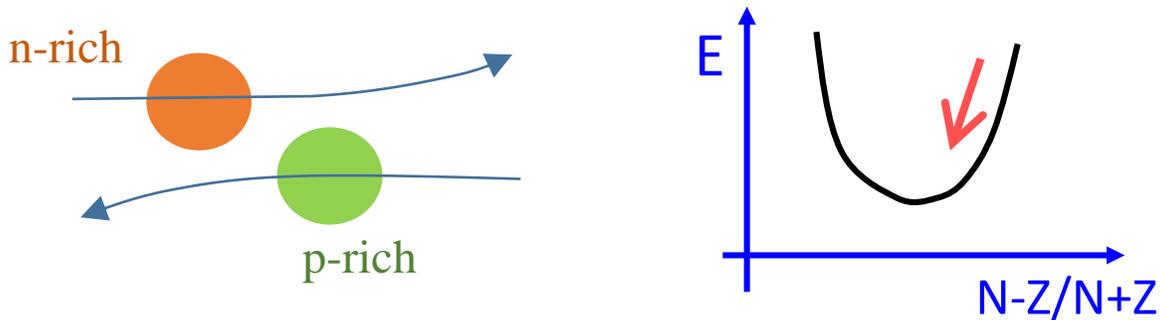


Two mechanisms governs the transport of IDOF in nuclear collisions:

1. Isospin Diffusion :

$$j_{np} = j_n^I - j_p^I = -(D_n^I - D_p^I) \nabla I$$

$$D_n^I - D_p^I \propto 4\rho E_{sym}(\rho)$$



Likely terminated when P-T separated.

2. Isospin Drift :

$$j_{np} = j_n^\rho - j_p^\rho = (D_n^\rho - D_p^\rho) \nabla \rho$$

$$D_n^\rho - D_p^\rho \propto 4I \frac{\partial E_{sym}(\rho)}{\partial \rho}$$



Likely persists for long time.

**Beam time: 6-13 Feb., 2018; Reaction: Ar+Au at 30 MeV/u;
Experimental site: RIBLL @ HIRFL**

Collaboration groups:

**Jiansong Wang's
IMP, CAS**

**Limin Duan's
IMP, CAS**

**Hongwei Wang's
SINAP, CAS**

